NPS67-82-002

NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

16-INCH GUN-LAUNCHED ANTI-SATELLITE WEAPON

by

Joseph John Natale

June 1982

Thesis Advisor:

A. E. Fuhs

Approved for public release, distribution unlimited

Prepared for:

Defense Advanced Research Projects Agency 1400 Wilson Boulevard Arlington, va 22209

82 09 16 004

NAVAL POSTGRADUATE SCHOOL Monterey, California

Rear Admiral J. J. Ekelund Superintendent

David Schrady Acting Provost

This thesis prepared in conjunction with research supported in part by the Defense Advanced Research Project Agency.

Reproduction of all or part of this report is authorized.

Released as a

Technical Report by:

W. M. Tolles

Dean of Research

SECURITY CLASSIFICATION OF THIS PAGE (When Date Ente

REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS BEFORE COMPLETING FORM
NPS 67-82-002 2. 419	308 3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subville) 16-Inch Gun-Launched Anti-Satellite Weapon	June 1982
-	NPS 67-82-002
7. Authory Joseph John Natale	ARPA Order No. 4035
Naval Postgraduate School Monterey, California 93940	PROGRAM ELEMENT PROJECT YASK AREA & WORK UNIT NUMBERS Program Element N062702E
Naval Postgraduate School Monterey, California 93940	12. REPORT DATE June 1982 13. NUMBER OF PAGES 92
Defense Advanced Research Projects 1400 Wilson Blvd.	Agency UNCLASSIFIED
Arlington, VA 22209	154. DECLASSIFICATION/DOWNGRADING

Approved for public release, distribution unlimited

- 17. DISTRIBUTION STATEMENT (of the abetract entered in Block 20, if different from Report)
- 18. SUPPLEMENTARY NOTES
- 19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

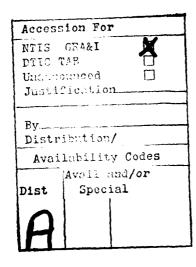
Gun-Launched, ASAT, Anti-Satellite

20. ABSTRACT (Continue on reverse side if necessary and identify by block number)

This thesis determined the feasibility of developing a 16-inch, gun-launched anti-satellite weapon. The general performance capability of rocket-and scramjet-boosted, gun-launched vehicles is examined with regards to propelling a miniature homing vehicle to a satellite intercept altitude. Rocket and scramjet boost vehicle performance is modeled and optimum trajectories are determined. A low gun elevation at launch and a pop-up manuever

FORUMTY CLASSIFICATION OF THIS RAGE/When Pole Balance

are required to maximize the scramjet boost vehicle acceleration potential. The rocket boost vehicle is capable of intercepting a low altitude satellite without a pop-up manuever from a gun elevation of 45 degrees. Both boost methods provide apogees consistent with the intercept of known Soviet Electronic Intelligence Ocean Reconnaissance satellites, EORSAT, and Radar Ocean Reconnaissance satellites, RORSAT.





Approved for public release, distribution unlimited

16-Inch Gun-Launched Anti-Satellite Weapon

bу

Joseph John Natale Lieutenant, United States Navy B.A., University of California, Los Angeles, 1975

Submitted in partial fulfillment of the requirement for the degree of

MASTER OF SCIENCE IN ENGINEERING SCIENCE

from the

NAVAL POSTGRADUATE SCHOOL June 1982

Author:

Approved by:

Approved by:

Chairman, Department of Aeronautics

Dean of Science and Engineering

ABSTRACT

This thesis determines the feasibility of developing a 16-inch, gun-launched anti-satellite weapon. The general performance capability of rocket-and scramjet-boosted, gun-launched vehicles is examined with regards to propelling a miniature homing vehicle to a satellite intercept altitude. Rocket and scramjet boost vehicle performance is modeled and optimum trajectories are determined. A low gun elevation at launch and a pop-up manuever are required to maximize the scramjet boost vehicle acceleration potential. The rocket boost vehicle is capable of intercepting a low altitude satellite without a pop-up manuever from a gun elevation of 45 degrees. Both boost methods provide apogees consistent with the intercept of known Soviet Electronic Intelligence Ocean Reconnaissance satellites, EORSAT, and Radar Ocean Reconnaissance satellites, RORSAT.

TABLE OF CONTENTS

I.	INT	RODU	CTION	7
II.	BAC	KGRO	UND AND DEVELOPMENT	8
	Α.	THE	MINIATURE ANTI-SATELLITE VEHICLE	8
	В.	THE	16-INCH, 50-CALIBER NAVAL GUN	8
	c.	16-	INCH GUN ASAT WEAPON	10
		1.	Target Altitudes	10
		2.	Mission Profile	10
		3.	Physical Characteristics	12
III.	воо	ST V	EHICLE	13
	Α.	SCR	AMJET	14
		1.	Scramjet Background	14
		2.	Scramjet Model	14
			a. Compustor	15
			b. Inlet	22
			c. Scramjet Thrust Data	26
			d. Curve Fit for Scramjet Performance	26
			e. Scramjet Vehicle Design	29
	В.	ROC	KET	33
		1.	Rocket Background	33
		2.	Rocket Model	33
			a. Rocket Thrust	33
			b. Rocket Vehicle Design	34

IV. HYPERSON	NIC AERODYNAMICS	36
A. HYPI	ERSONIC AERODYNAMIC FORCES	36
1.	Case One: A7=0	38
2.	Case Two: A7 <a3< td=""><td>38</td></a3<>	38
3.	Case Three: A7>A3	38
4.	CD and CL	41
B. CONT	TROLS	43
1.	Forms of Control	43
V. TRAJECTO	ORY OPTIMIZATION	45
A. OPT	IMUM SCRAMJET TRAJECTORY	45
B. OPTI	IMUM ROCKET TRAJECTORY	49
VI. CONCLUS	IONS	53
APPENDIX A - I	PROGRAM LISTING FOR SCRAMJET THRUST	54
APPENDIX B - 1	FI-59 SCRAMJET PROGRAM OUTPUT	60
	GUN-LAUNCHED SCRAMJET/ROCKET ASAT MISSION PROFILE, PROGRAM LISTING	63
I	GUN-LAUNCHED SCRAMJET ASAT APOGEE AS A FUNCTION OF GUN ELEVATION, ANGLE-OF-ATTACK AND POP-UP ALTITUDE	73
APPENDIX E - N	MAXIMUM APOGEE TRAJECTORY LISTINGS	79
LIST OF REFERE	ENCES	88
BIBLIOGRAPHY	*	90
TNITMIAI DIOMBI	TRUMTON I TOP	0.1

I. INTRODUCTION

There are four events which suggest that a feasibility study should be made of the 16-inch naval gun as an antisatellite, ASAT vehicle launcher. The first event is the paper by A. M. Valenti, Sannu Molder and G. R. Salter [Ref. 1] which indicates that a gun-launched supersonic-combustion ramjet, scramjet, is capable of 50-g acceleration and Mach 15 velocity. There is also the paper by C. H. Murphy, G. V. Bull and E. D. Boyer [Ref. 2] which indicates that a gun-launched rocket is capable of placing a payload in a highly elliptical 19,000 nm by 500 nm orbit. The second event is the U.S. Air Force development of a rocket-propelled, miniature ASAT weapon to be launched from the F-15 aircraft [Ref. 3]. third event is the recommissiong of at least one Iowa class Battleship, consequently bringing nine 16-inch guns into service. The fourth event is the proliferation of long range anti-ship cruise missiles. To survive, a Naval Task Group must deny the enemy over-the-horizon targeting information provided by Ocean Surveillance Satellites [Ref. 4].

The USAF ASAT system involves the placement of a Miniature Vehicle, MV, which is a highly sophisticated homing weapon, in a sub-orbital acquisition window [Ref. 3]. The problem is, can a 16-inch, gun-launched vehicle place this or a similar MV ASAT weapon in the required sub-orbital acquisition window?

II. BACKGROUND AND DEVELOPMENT

A. THE MINIATURE ANTI-SATELLITE VEHICLE

Aviation Week [Ref. 3] describes the USAF ASAT as:

Miniature vehicle anti-satellite weapon under development by the U.S. AIR FORCE SPACE DIV and Vought would utilize long wave infrared homing combined with laser-gyro stabilization and an extensive lateral maneuvering capability to collide with and destroy a hostile Soviet spacecraft.[p. 243]

The Air Force system actually uses the F-15 aircraft as a first stage; a Boeing short-range attack missile (SRAM) and a Vought Altair are used as second and third stage vehicles. The F-15 flies to a predetermined position and altitude and launches the SRAM-Altair-MV vehicle. The SRAM provides the majority of accelration. The second stage Altair spins the MV to 20 revolutions a second. After the target has been acquired by the MV, the MV is released by the Altair. The MV is described as being approximately 12 x 13 inches in size. [Ref. 3]

B. THE 16-INCH, 50-CALIBER NAVAL GUN

The 16-inch, 50-caliber naval gun, like the nine aboard the USS NEW JERSEY, has a 16-inch diameter bore. The barrel is approximately 66 feet long. The maximum gun elevation is 45 degrees. Standard projectiles weigh about 2700 pounds with a typical muzzle velocity of 2800 feet per second [Ref. §]. The values above vary with charge and projectile weight.

Performance of the 16-inch gun when projectiles with smaller mass are used can be predicted. Assuming a frictionless barrel, which should be nearly feasible with silicon or teflon coated projectiles,

$$U = (\frac{P}{m} 2AL)^{1/2}$$
 (1)

P = average pressure on the base of the projectile

m = mass of the projectile

A = base area of projectile

L = length of barrel U = muzzle velocity

Using P = $1.58562 \times 10^8 \text{ N/m}^2$ or 23,000 lbf/in², A = 0.1297 m^2 , and L = 20.32 m, the Mach number as a function of projectile mass is:

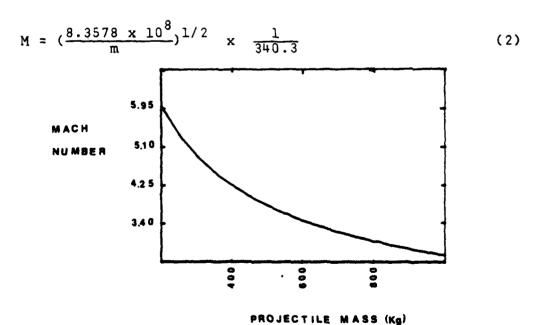


Fig. 1: MUZZLE MACH NUMBER VS. PROJECTILE MASS
The results of Figure 1 are substantiated by D. Monetta [Ref. 6].

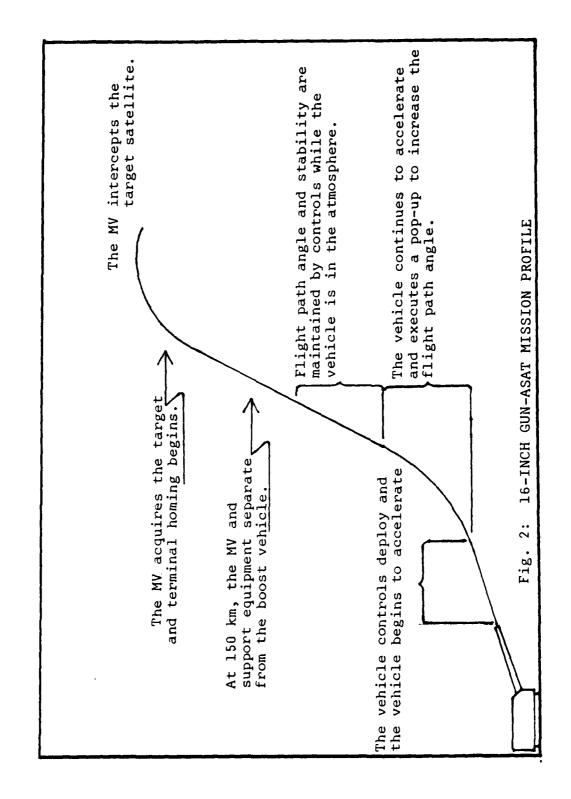
C. 16-INCH GUN ASAT WEAPON

1. Target Altitudes

Ocean reconnaissance and targeting satellites are presumedly the primary targets for a Naval ASAT system [Ref. 3]. Their ability to locate and identify ships simplifies the Soviet over-the-horizon targeting problem. The Soviet RORSAT, Radar Ocean Reconnaissance Satellite, orbits at an altitude between 250 Km and 260 Km. The Soviet EORSAT, Electronic Intelligence Ocean Reconnaissance Satellite, orbits at an altitude between 430 Km and 440 Km [Ref. 4]. The altitude achieved by the gun-launched ASAT should be sufficient to intercept these satellites.

2. Mission Profile

Figure 2 depicts a possible 16-inch gun-launched ASAT mission profile. The 16-inch gun performs the function of a first stage booster, accelerating the boost vehicle, which includes the miniature ASAT vehicle, MV, to a velocity between Mach 3 and Mach 5. The boost vehicle should accelerate to a velocity between Mach 7 and Mach 9 and increase the flight path angle as measured from the horizontal to between 50 and 85 degrees. The MV and support equipment wi'l detach from the boost vehicle at 150 Km. As the MV approaches the apogee, target acquisition occurs and lateral guidance corrections are made as necessary to achieve an intercept [Ref. 3].



3. Physical Characteristics

The boost vehicle may have a di meter as large as 16.5 inches if the gun is fitted with a smooth bore liner. A smooth bore in one of the nine 16-inch barrels on the Iowa class Battleship would not significantly degrade the ship's firepower. A smooth bore gun may also find additional applications with gun launched guided projectiles.

The vehicle may be sub-caliber if saboted; however, a sub-caliber vehicle with a diameter less than 14 inches will not accommodate the existing MV. The length of the vehicle is governed by the amount of handling room in the gun turret, by the barrel length and by the ability of the vehicle structure to withstand loading due to acceleration in the gun. The standard 16-inch projectile is approximately 80 inches long. Assuming the boost vehicle can be sectioned and assembled while being loaded into the gun, it could reasonably be 192 inches long [Ref. 2]. Acceleration within the barrel will range from 2600-g's to 7200-g's. The duration of this peak loading is from 0.04 to 0.02 seconds. If 120% yield stress is used as a working stress, it is reasonable to predict that 50 - 75% of the vehicle weight will be required for the structure [Ref. 1].

III. BOOST VEHICLE

The compatability of the boost vehicle with the 16-inch gun-launcher dictates many of the vehicle characteristics. Primarily, the vehicle is volume limited. The vehicle mass is also a key factor. The vehicle mass, as in any missile, is a function of payload, fuel, structure and controls; however, in this specialized application, mass also affects the muzzle velocity, V_0 . Assuming vehicle with a mass of 350 Kg is used, the V_0 obtainable is 1360 m/sec, which is Mach 4.5. For the EORSAT mission, the intercept trajectory requires the vehicle to be at a velocity of 2618 m/sec, V, at 10 Km altitude. To achieve the required velocity, the vehicle must be capable of 7.9-g's of acceleration, A.

$$\frac{A}{g_0} = \frac{(v - v_0)^2}{2g_0 h}$$
 (3)

Muzzle velocity may be increased, thereby reducing the acceleration requirements. However, an increase in V_0 is at the expense of fuel and/or payload. The required strength and consequently the mass of the vehicle case can only increase with increased V_0 .

The majority of the air breathing engines are not applicable as a result of their inherent performance limitations.

This includes the subsonic combustion ramjet, due to a low

acceleration limit. The supersonic combustion ramjet, scramjet, is, however, theoretically capable of 50-g acceleration [Ref. 1].

Solid or liquid fuel rockets of single-or multi-stage design are a second potential souce of propulsion.

A. SCRAMJET

1. Scramjet Background

Considerable research was focused on scramjets during the late 60's and early 70's. This included the testing of a Mach 7.0 gun-launched scramjet in 1975 [Ref. 7]. The detailed analysis required to develop a completely accurate model of a scarmjet is beyond the scope of this thesis. Therefore, various assumptions are made to simplify the scramjet model. The goal is to first determine system feasibility and to second identify areas requiring additional study.

Scramjet Model

The first assumption in this model is that γ , the ratio of the heat capacities, is constant and equal to 1.4 throughout the scramjet. Admittedly this is an erroneous assumption as the temperatures and pressures involved exceed the realm of ideal gas. Never-the-less the straight-forward evaluation allowed by the use of equations for ideal gas provides an optimistic, yet relevant, performance base-line for overall scramjet boosted ASAT system evaluation.

The scramjet was modeled in two sections, inlet and combustor. The nozzle is assumbed to be capable of expanding the flow to the ambient pressure, P_0 , at all altitudes. The inlet is assumed to have variable geometry which will maintain a constant ratio of M_3/M_0 for all values of M_0 . This performance characteristic is assumed to be achievable and is derived to maximize the thrust [Ref. 8]. The design of this inlet may, in fact, not be feasible and is an area requiring additional study.

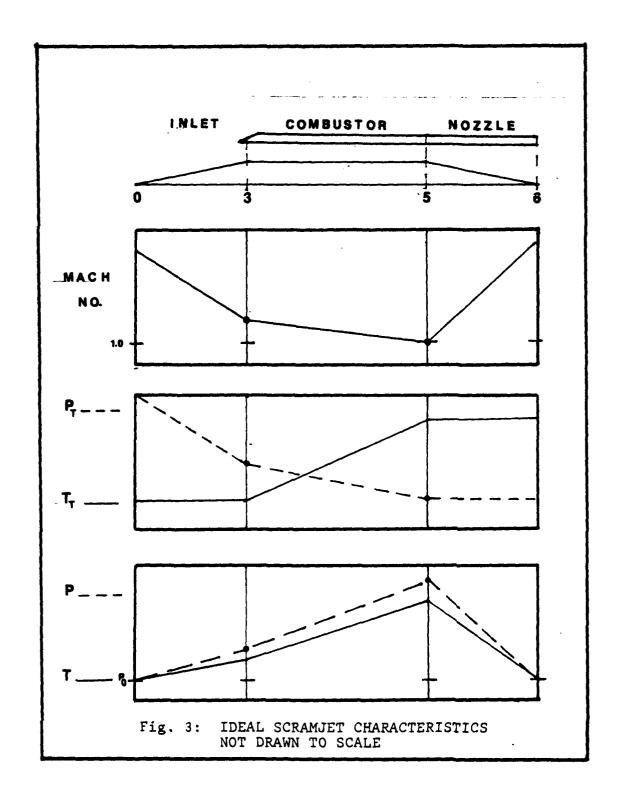
a. Combustor

As shown in Figure 3, air enters the combustor at point 3 at some Mach number, M_3 . M_3 is a function of the free stream Mach number, M_0 , the kinetic energy efficiency of the diffuser, η_d , and some stagnation pressure, P_{T3} . P_{T3} is a function of the ratio of P_{T3}/P_{T0} , π_d . If P_{T3}/P_{T0} = π_d , P_{T5}/P_{T3} = π_b and P_{T6}/P_{T5} = π_n and complete expansion is assumed in the nozzle, then

$$\frac{P_{T6}}{P_{T0}} = \pi_n \times \pi_b \times \pi_d \tag{4}$$

Static and stagnation pressures at entrance and exit are related by

$$P_{6} = P_{0} = \frac{P_{T6}}{\left[1 + \frac{\gamma - 1}{2} M_{6}^{2}\right]^{\frac{\gamma}{\gamma - 1}}} = \frac{P_{T0}}{\left[1 + \frac{\gamma - 1}{2} M_{0}^{2}\right]^{\frac{\gamma}{\gamma - 1}}}$$
(5)



From equations (4) and (5):

$$\frac{P_{T0}(\pi_n \pi_b \pi_b)}{[1+\frac{\gamma-1}{2} M_6^2]^{\frac{\gamma}{\gamma-1}}} = \frac{P_{T0}}{[1+\frac{\gamma-1}{2} M_0^2]^{\frac{\gamma}{\gamma-1}}}$$
(6)

Let

$$\pi = [\pi_n \ \pi_b \ \pi_d] \frac{\gamma - 1}{\gamma} = \frac{1 + \frac{\gamma - 1}{\gamma} \ M_6^2}{1 + \frac{\gamma - 1}{\gamma} \ M_0^2}$$
 (7)

and TR = 1 + $[(\gamma+1)/2] M_0^2$.

Solving equation (7) for $(M_6/M_0)^2$ and relating Mach number and temperatures, results in equation (8).

$$\left(\frac{M_6}{M_0}\right)^2 = \left(\frac{V_6}{V_0}\right)^2 \cdot \frac{T_0}{T_6} = \frac{1}{TR-1} (TR \cdot \pi - 1)$$
 (8)

The energy equation across the combustor is

$$Q + \sum_{inlet} \dot{m}_{i} h_{Ti} = \sum_{exhaust} \dot{m}_{e} h_{Te}$$
(9)

where $\hat{Q} = [fuel flow rate]x[chemical energy of the fuel (h_f, BTU/lbm)]x[the combustion efficiency (n_b)]. Applying the definitions above to the energy equation produces equation (10).$

$$f h_f \eta_b + h_{T3} = (1+f) h_{T6}$$
 (10)

By relating the stagnation temperature to the enthalpy by $h_T = C_p T_T$, and solving for the fuel-air ratio, f, equations (11) and (12) may be written as:

$$C_{p}T_{T0} = f h_{f} n_{b} = (1+f)C_{p}T_{T6}$$
 (11)

$$f = \frac{\frac{T_{T5}}{T_{T0}} - 1}{\frac{h_{f} n_{b}}{C_{p} T_{T0}} - \frac{T_{T5}}{T_{T0}}}$$
(12)

As indicated in Figure 3, the stagnation temperature, T_T , at point 0 is equal to the stagnation temperature at point 3, therefore, from equation (12):

$$\frac{T_{T5}}{T_{T0}} = \frac{T_{T5}}{T_{T3}} = 1 + \frac{fh_f n_b (1+f)}{C_p T_{T0}}$$
 (13)

Solving for the Mach number at point 5 from equation (13):

$$M_5^2 = \frac{(1-2\gamma M_3^2 K) + \sqrt{1-2KM_3^2(\gamma+1)}}{(2M_3^2 \gamma^2 K - \gamma - 1)}$$
(14)

where

$$K = \frac{T_{T5}}{T_{T0}} \left(\frac{1 + \frac{\gamma - 1}{2} M_3^2}{(1 + \gamma M_3^2)^2} \right)$$
 (15)

Now π_b may be expressed as:

$$\pi_{b} = \frac{P_{T5}}{P_{T3}} = \frac{1 + \gamma M_{3}^{2}}{1 + \gamma M_{5}^{2}} \left(\frac{1 + \frac{\gamma - 1}{2} M_{5}^{2}}{1 + \frac{\gamma - 1}{2} M_{3}^{2}} \right)$$
(16)

In evaluating π_d , the kinetic energy efficiency of the diffuser, n_d , is defined by stream velocity at roint 3, V_3 , divided by the free stream velocity, V_0 , quantity squared. This assumes isentropic expansion to the free stream pressure P_0 for a given h_{T3} and P_{T3} [Ref. 8]. As developed by G. L. Dugger [Ref. 8], given M_3 , P_{T3} may be determined from:

$$n_d = 1 - \frac{(\frac{P_{T0}}{P_{T3}})^{\frac{\gamma-1}{\gamma}} - 1}{(\frac{\gamma-1}{2} M_0^2)}$$

Therefore π_d may be expressed as:

$$\pi_{d} = (1 + \frac{\gamma - 1}{2} M_0^2 (1 - \eta_d))^{-(\frac{\gamma}{\gamma - 1})}$$
 (17)

 P_{T6}/P_{T5} , π_n , is assumed to be equal to 0.9.

$$F = \dot{m}_6 V_6 - \dot{m}_0 V_0 + A_6 (P_6 - P_0)$$
 (18)

The general equation of thrust for an air breathing engine, above, may be written as equation (22) by assuming complete expansion in the nozzle such that $P_6 = P_0$. Then writing F as,

$$F = \dot{m}_0 V_0 \left(\frac{\dot{m}_6 V_6}{\dot{m}_0 V_0} - 1 \right) \tag{19}$$

and noting that from equation (8)

$$\frac{V_{6}}{V_{0}} = \frac{M_{6}}{M_{0}} \sqrt{\frac{T_{6}}{T_{0}}} = \sqrt{\frac{1}{TR-1}(TR \cdot \pi - 1) \frac{T_{6}}{T_{0}}}$$
 (20)

 $\dot{m}_6 = \dot{m}_{air} + \dot{m}_{fuel}$ such that $\dot{m}_6/\dot{m}_0 = (1+f)$ by definition. Substituting equations (13) and (7) into the expression for T_6/T_0 in terms of stagnation temperature results in:

$$\frac{T_6}{T_0} = \frac{1 + \frac{f h_f \eta_b}{C_p T_{T0}}}{\pi (1+f)}$$
 (21)

Combining and simplifying equation (19), (20), and (21) results in equation (22).

$$F = \dot{m}_0 V_0 \left(\sqrt{\frac{(1+f)(TR \cdot \pi - 1)(1 + \frac{f\eta_b h_f}{C_p T_{T0}})}{\pi (TR - 1)}} - 1 \right)$$
 (22)

Equation (22) is the expression for thrust produced by a scramjet as a function of M_0 , M_3 , losses in the engine π , f, n_b , h_f , \dot{m}_0 , and T_{T0} .

The equations for thrust as a function of altitude M_0 and M_3 , were programmed for a TI-59 calculator. See Appendix A for program listing. The atmospheric variable, ρ_0 (air density lbm/ft³), T_0 (static air temperature, °R) and a_0 (sonic velocity, ft/sec) were entered for each altitude from tables of the ICAO STANDARD ATMOSPHERE [Ref. 9].

Though liquid hydrogen would provide a greater $I_{\rm sp},$ a carbon-based fuel is used in this model. Carbon-based

fuels, like JP-5, $C_{10}H_{19}$, may be easily adapted to shipboard storage and have a significant density advantage over liquid hydrogen. The density of the fuel utilized is critical in this volume-limited system. The h_f used in these calculations is 18630 Btu/lbm. The flame temperature in the combustor, T_5 , for JP-5 in air at 1500°R and 40 atmospheres is approximately 5000°R. The air temperature and pressure are approximations for conditions of point 3 when M_0 is Mach 6 at sea level. The theoretical stoichiometric f for JP-5 is 0.0687; f for the maximum flame temperature above is 0.0733. The flame temperature, T_5 , of 5000°R is used as a limiting factor in the thrust equation.

The thrust program, illustrated in Figure 4 and summarized in Table I, is a decremental-loop program which decrements the value of f and then determines; one, if M_5 can be calculated; two, if M_5 is approximately equal to 1.0; and three, if T_5 is within the limits for combustion of JP-5. Failure of any of the three tests results in a reduction of f and another attempt at calculating the thrust. The test for $M_5 \ge 1$ causes the thrust to be determined for thermally choked flow at point 5. Thermally choked flow for a constant area combustor provides maximum thrust and over-all engine efficiency [Ref. 8].

b. Inlet

A significant factor governing the amount of thrust produced is the Mach number of the flow at point 3,

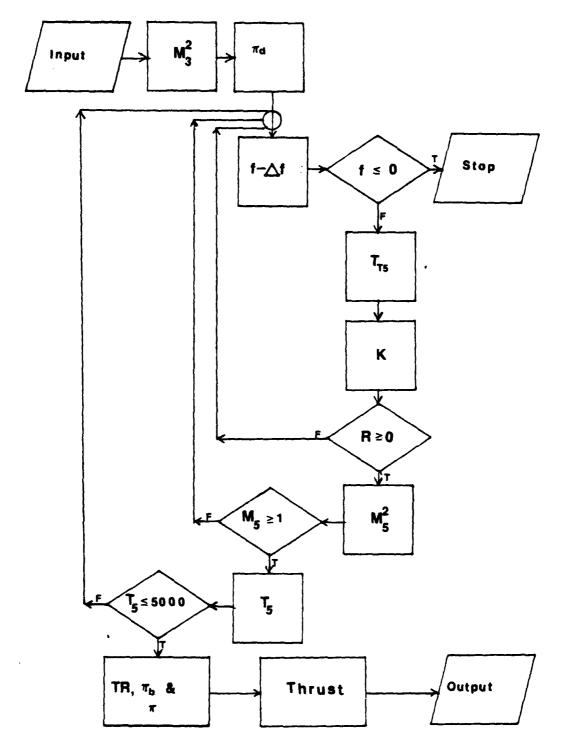


Fig. 4: SCRAMJET THRUST PROGRAM, LOGIC FLOW CHART

TABLE I

SUMMARY OF SCRAMJET THRUST PROGRAM EQUATIONS

$$\pi_d = (1+0.2M_0^2(1-\eta_d)^{3.5}$$

$$M_3 = 0.7M_0$$

$$\eta_b = 0.982$$

$$T_{T5} = \frac{(f 76950 + T_{T0})}{(1+f)}$$

$$K = (\frac{T_{T5}}{T_{T0}}) (\frac{1+0.2M_3^2}{(1+1.4M_3^2)^2})$$

$$R = (1-4.8KM_3^2)$$

$$M_5 = \sqrt{\frac{2.8M_3^2 K - 1 - \sqrt{R}}{(0.4 - 3.92M_3^2 K)}}$$

$$TR = (1+0.2M_0^2)$$

$$\pi_{b} = \frac{(1+1.4M_{3}^{2})}{(1+1.4M_{5}^{2})} \left[\frac{(1+0.2M_{5}^{2})}{(1+0.2M_{3}^{2})} \right]^{3.5}$$

$$\pi = (\pi_{n} \pi_{b} \pi_{d})^{0.286}$$

$$F = \rho_{0} A V_{0}^{2} \left[\sqrt{\frac{(1+f)(TR \cdot \pi - 1)(1 + \frac{f \eta_{b} h_{f}}{C_{p} T_{T0}})}{\pi (TR - 1)}} - 1\right]$$

 ${
m M}_3$. Thrust was maximized for this scramjet by calculating thrust as a function of ${
m M}_3$ for various values of ${
m M}_0$, see Figure 5. Thrust was found to be maximized when ${
m M}_3/{
m M}_0 \simeq 0.7$. Figure 5 was determined for sea level; however, the results were determined to be reasonably consistent at various altitudes.

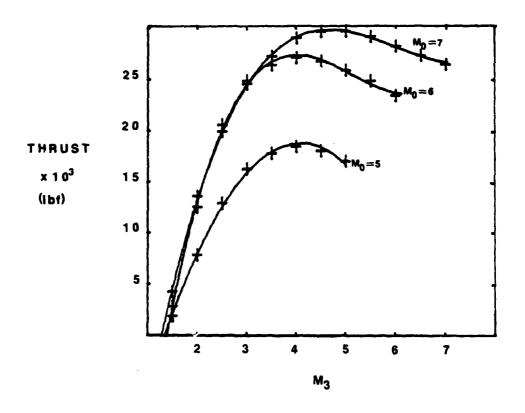


Fig. 5: SCRAMJET THRUST AS A FUNCTION OF THE MACH NUMBER AT POINT 3, M3

The kinetic efficiency of the diffuser $\eta_{\rm d}$ was determined with the equation $\eta_{\rm d}$ = 0.94 + 0.06M $_3/{\rm M}_0$. This

equation assumes perfect air through a 3 oblique shock inlet with wedge angles of 10 to 15 degrees for Mach numbers from 3.0 to 7.0 [Ref. 8].

c. Scramjet Thrust Data

The thrust produced by the scramjet was calculated as a function of \mathbf{M}_0 and altitude with the following variables set to the values indicated:

The results are presented in Appendix B.

d. Curve Fit for Scramjet Performance

requires the values for thrust and fuel flow at
each point along the flight path. The increment loop nature
of the thrust program makes its incorporation into a flight
path program undesirable. Fortunately, the plots of thrust
and f as a function of Mach number and altitude are adequately
represented by a series of straight lines. Figure 6 presents
the correlation between the calculated data points, which are

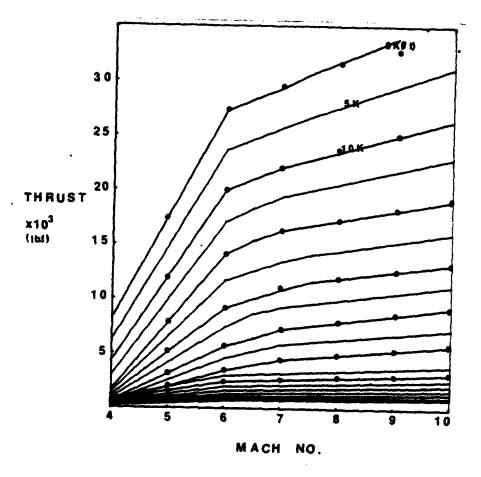


Fig. 6: SCRAMJET THRUST AS A FUNCTION OF MACH NUMBER AND ALTITUDE

shown as large dots calculated with the TI-59 thrust program, and the thrust curves calculated with the linear equations based on the thrust data. The linear equations for thrust are rather tedious and may be found in the program listing, Appendix C. The graph of f as a function of Mach number and altitude, shown in Figure 7, indicates that f may be approximated by three linear equations:

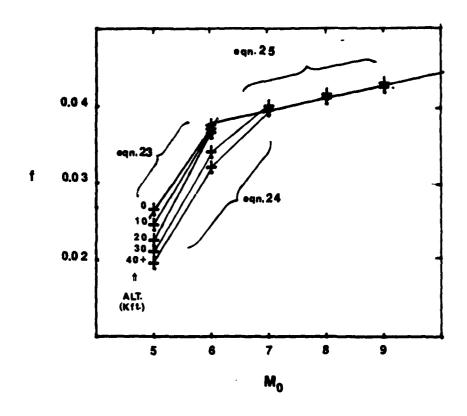


Fig. 7: FUEL-AIR RATIO, f, AS A FUNCTION OF THE MACH NUMBER AT POINT 0, M, AND ALTITUDE WITH CORRELATION TO APPROXIMATING EQUATIONS (23), (24), (25)

f =
$$0.011(M-5) + 0.0266$$

where $4 \le M_0 \le 6$ and altitude < 30,000 ft. (23)

f =
$$0.0093(M-5) + 0.021$$

where $4 \le M_0 < 7$ and altitude > 30,000 ft. (24)

f =
$$0.0017(M-6) + 0.037$$

where 1) $M_0 > 6$, altitude < 30,000 ft.
2) $M_0 > 5$, altitude > 30,000 ft. (25)

e. Scramjet Vehicle Design

A complete and thorough design for a gun-launched ASAT using a scramjet far exceeds the scope of this thesis. However a general dimensional presentation is required to determine aerodynamic characteristics as well as fuel and payload volume capacity.

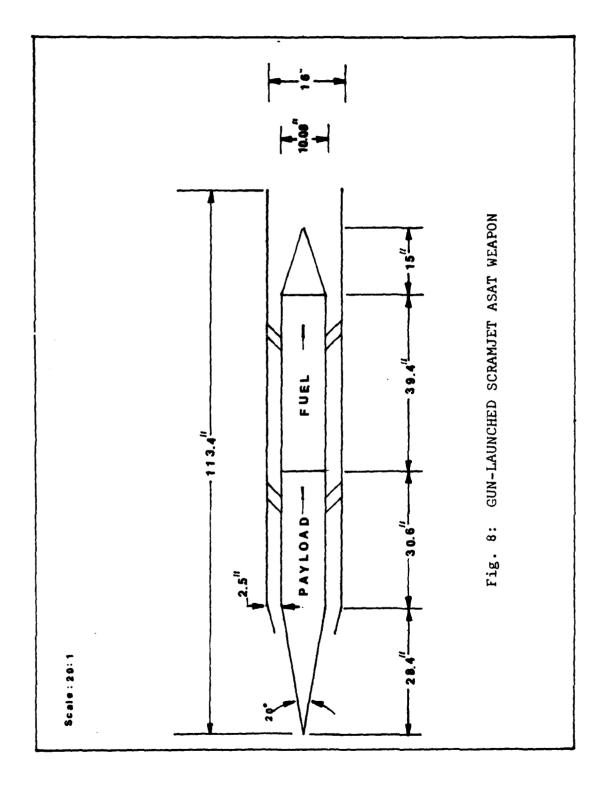
The three-dimensional parameters that generally define the shape and size of the vehicle are outer diameter, inner diameter and length. The outer diameter is established by the gun which is 16 inches if the gun is unaltered and 16.5 if the rifling is removed. Total length assuming the capability of performing some assembly of diffuser and tail section in the gun turret should be a maximum of about 16 feet. The inner diameter refers to the diameter of the cylindrical inner body which houses the payload, fuel and the vehicle controls. The inner diameter (i.e., the diameter of the center body) is influenced by two factors. The first factor is a result of the design characteristics of the diffuser. A minimum area at point 3, A_3 , exists with regards to the free stream capture area, \mathbf{A}_0 , and \mathbf{M}_0 . Continuing with the assumptions of ideal gas, $M_3/M_0 = 0.7$ and $\eta_d = 0.982$ the ratio A_3/A_0 may be obtained as follows: by continuity \dot{m}_0 = \dot{m}_3 such that $A_3/A_0 = (P_0/P_3)(M_0/M_3)(A_0/A_3)$. From the relationships for ideal gas the $T_{T0} = T_{T3}$, $P_{T0}/P_{T3} = 1/\pi_d$ the ratio of A_3/A_0 may be written as:

$$\frac{A_3}{A_0} = \frac{1}{\pi_d} \frac{M_0}{M_3} \left(\frac{1 + \frac{\gamma - 1}{2} M_3^2}{1 + \frac{\gamma - 1}{2} M_0^2} \right) (\frac{\gamma}{\gamma - 1} - 1)$$
 (26)

Evaluating $1/\pi_d$ with equation (17) and applying the assumptions above, A_3/A_0 may be calculated as a function of M_0 . At this point, an assumption must be made about the thickness of the outer case illustrated in Figure 8. Obviously, for a fixed A_0 , the ratio of the diameter of the center body to free stream capture area, A_3/A_0 , must decrease as the outer case thickness increases. Therefore, at least two options exist. The first option is to make the outer case thick enough to hold the fuel and controls. The second option minimizes the thickness of the outer case and carries all fuel and controls in the center body. The payload section will necessarily be located in the center body of the boost vehicle. The center body is required to be at least 13 inches in diameter to accommodate the existing ASAT MV or have sufficient volume to accommodate a volume-equivalent ASAT MV. Option two is therefore applicable.

If the outer case wall is assumed to be 0.5 inches thick, the area within the outer case is 176.7 square inches. For an A_0 of 153.9 square inches and flight Mach numbers of 4.5 to 9.0, A_3 will vary from 61.56 to 96.96 square inches.

Assuming the variable geometry of the inlet assembly is capable of reducing A_2 from its maximum to its



minimum value, the maximum center body area must be small enough to provide for the maximum A_3 . Consequently, the center body is limited to a 10.08 inch diameter.

As the dimensions of the center body will not accommodate the existing ASAT MV, a volume-equivalent pay-load of 2261 cubic inches will be used. This volume includes the 12 x 13 inch cylindrical MV and an additional 790 cubic inches of auxillary equipment.

Figure 8 is a general representation of a potential gun-launched scramjet ASAT vehicle. The volume equivalent payload will occupy the 309 cubic inches of the diffuser cone as well as a 30.6 inch section of the center body. This assumes 0.5 inch thick walls and a 10.08 inch diameter center body.

The scramjet engine was modeled using JP-5 as a typical fuel. JP-5 has a density of 0.0296 lbm/in³. Therefore, to carry 100 lbm of fuel requires 3376.3 cubic inches; based on center body diameter, the volume corresponds to a 52.6 inch long section of center body. If a high density carbon based fuel, similar to the fuels being developed for various cruise missile applications, is used, a fuel density of 0.0397 lbm/in³ may be assumed [Ref. 10]. The center body length required for fuel is then reduced to 39.4 inches. The vehicle case including structure and insulation is assumed to have an average density of 0.0367 lbm/in³. The assumed total case mass is 356.33 lbm. Fuel

allotted is 110.23 lbm. The payload, which includes the MV, and support equipment, is allotted 100 lbm. Control and guidance equipment which includes diffuser control, fuel control and control surfaces actuators is allotted 15 lbm. Vehicle total launch weight is 716.5 lbm.

B. ROCKET

1. Rocket Background

Gun launched sounding rockets have been developed and tested as part of several projects. During the late 60's and early 70's, the Gun-Launched-Orbitor, (GLO-IA), was developed [Ref. 2]. The GLO-IA was a three stage system designed to be fired from a 16.7 inch, 75 caliber gun. The predicted apogee with a 8.6 lbm payload was 2629 nm. Applying this promising performance to the ASAT problem resulted in the following model.

Rocket Model

The rocket boosted gun-launched ASAT is a simple, single stage, fin-controlled system. The design assumes a smooth bore oversized gun barrel. The vehicle is assumed to be 16.5 inches in diameter. If a silicon greased nylon, or teflon obturator, is used, the barrel will be approximately 16.7 inches in diameter.

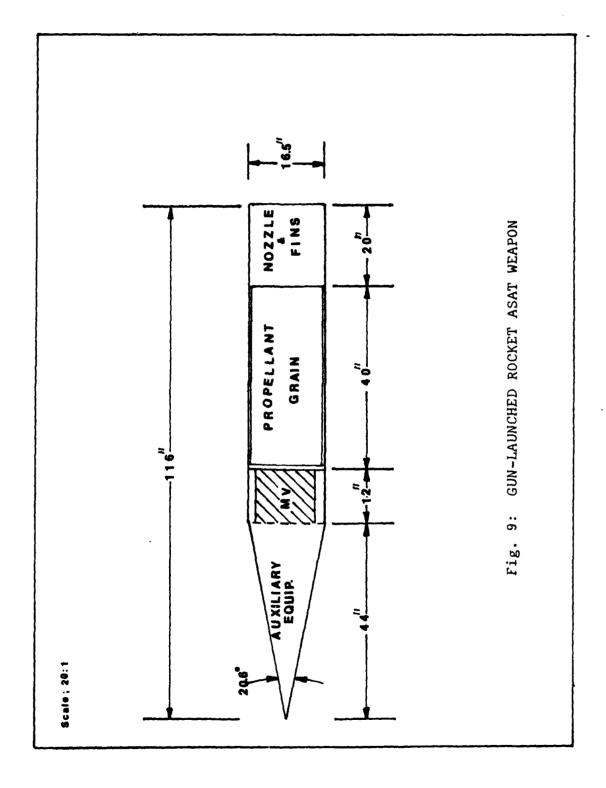
a. Rocket Thrust

The propellant grain is 40 x 16 inches, end inhibited, with an internal eight point star. A possible propellant is DB/AP-HMX/Al, which has a density of 0.067

lbm/in 3 . The boost grain mass is 472.2 lbm or 216 Kg. For the purposes of this model, thrust is assumed to be constant and equal to the average thrust. The average thrust, T, is equal to 19010 lbf or 84556.48 Nt. The $I_{\rm sp}$ is 243 sec. Propellant mass burn rate is 78.7 lbm/sec or 36 Kg/sec. Assuming the action time equals the burn time, the boost grain is modeled to produce the average thrust for 6 seconds. The model also assumes complete expansion in the nozzle.

b. Rocket Vehicle Design

The diameter of the rocket boost vehicle will allow the use of the MV developed for the Air Force. As illustrated in Figure 9, a 12-inch long section of vehicle is allotted for the MV. Additionally, 2421 cubic inches are available in the nose cone for auxiliary equipment. The payload mass in the rocket system is the same as the scramjet system, 100 lbm. The weight of the vehicle case and controls, based on the values given for the GLO-1B [Ref. 2] is 184.4 lbm or 83.6 Kg. Total vehicle mass is 760.59 lbm or 345 Kg.



IV. HYPERSONIC AERODYNAMICS

Both the scramjet and the rocket boost vehicles exit
the barrel at a high supersonic Mach number, 4.5, and
rapidly accelerate to hypersonic speeds greater than Mach 5.
Both vehicles are basically cone capped cylinders. As
indicated in Figure 2, in order to maximize performance,
the vehicles will need to increase their flight path angle,
A, from the maximum gun launch angle of 45 degrees. The
variables used in this section are those used in the trajectory program of Appendix C. Aerodynamic lift is used to
achieve the change in trajectory angle. The change in
trajectory angle is termed a pop-up maneuver. Therefore,
the aerodynamic control system for the vehicle must be
capable of providing an angle of attack, A7, as well as
stabilizing the vehicle.

A. HYPERSONIC AERODYNAMIC FORCES

One theoretical method of dealing with hypersonic aerodynamics is through the use of Newtonian impact theory. This entire section on hypersonic aerodynamics follows closely the presentation in Chapters 3 and 4 of Truitt [Ref. 11]. The basic assumption is that at extremely high Mach numbers the aerodynamic force coefficients are independent of the mach number. Aerodynamic forces on the body are a function of surface area presented to the free

stream. Comparison between impact theory predictions of force characteristics for a cone-cylinder body and experimental data at Mach 7 is of the same order of accuracy as obtained at lower Mach number with supersonic theory.

Accuracy can be expected to increase with higher Mach numbers as the impact theory is derived for a free stream Mach number of infinity.

Three possible cases can be considered in determining the force coefficients for the body:

Case One - The angle of attack equals zero, A7 = 0.

Case Two - The angle of attack is less than or equal to the half cone angle, A7<A3.

Case Three - The angle of attack is greater than the half cone angle, A7>A3.

Define the following symbols:

 C_M = normal force coefficient

C_C = axial force coefficient

A3 = half cone angle (deg)

A7 = angle of attack (deg)

R9 = diameter of cone base = diameter of cylinder(inch)

 L_{nL} = length of cone (inch)

 L_{DS} = length of cone not considered for cowl (inch)

R0 = diameter of cowl opening (inch)

Using the cone shown in Figure 9, A_3 would be 10.3°.

1. Case One: A7 = 0

The cylinder is parallel to the free stream, therefore, $^{\rm C}{}_{\rm N}$ (Cyl) = $^{\rm C}{}_{\rm C}$ (Cyl) = $^{\rm C}{}_{\rm L}$ = $^{\rm C}{}_{\rm D}$ = 0. The cone presents a symmetrical surface to the free stream, therefore:

$$C_{\text{cone}} = 2 \sin^2 A3 \tag{27}$$

The normal force coefficient is equal and opposite at each opposing point on the cone such that $C_{N(Cone)} = 0$.

2. Case Two: A7≤A3

In this case, the entire cone is presented to the flow such that:

$$C_{\text{N}_{\text{cone}}} = \cos^2 A 3 \sin 2A7 \tag{28}$$

and

$$C_{\text{Cone}} = 2\sin^2 A3 + \sin^2 A7 (1-3\sin^2 A3)$$
 (29)

3. Case Three: A7>A3

Only a portion of the cone is presented to the free stream forming a low pressure shadow over the remainder of the surface. The area subject to free stream impact is described by:

$$B = \arcsin(\frac{\tan A3}{\tan A7}) \tag{30}$$

Then

$$C_{N_{\text{cone}}} = \cos^2 A 3 \sin A 7 \left[\frac{B + \frac{\pi}{2}}{\pi} + \frac{1}{3\pi} \right]$$

$$x \cos B(\cot A7 \tan A3 + 2\tan A7 \cot A3)]$$
 (31)

and

$$C_{\text{Cone}} = 2\sin^2 A3 + \sin^2 A7(1-3\sin^2 A3)(\frac{B+\frac{\pi}{2}}{\pi})$$

$$+ \frac{3}{4\pi} \cos B \sin 2A7 \sin 2A3 \qquad (32)$$

For both cases two and three, the force coefficient on the cylinder are represented by $C_{\rm C}$ = 0 and

$$C_{N_{\text{cyl}}} = \frac{5.33}{\pi} \frac{L9}{R9} \sin^2 A7$$
 (33)

Equations (27) through (33) effectively describe the hypersonic forces on the rocket boost vehicle. However, the scramjet configuration, neglecting the diffuser cone, is best represented by a partial cone and a cylinder. The partial cone represents the scramjet cowl.

In modelling the cowl consider the cone divided into two cones. As illustrated by Figure 10, the large cone has a length, $L_{\rm DL}$, and a base diameter of R9. The small cone has a length, $L_{\rm DS}$, and a base diameter of R0. The cowl is

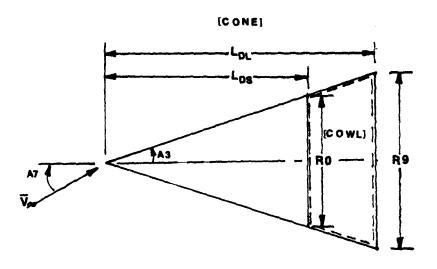


Fig. 10: CONE AND COWL

Converting to a common base area

$$C_{N_{Small Cone}} \left(\frac{\pi R0^2}{4} - \frac{4}{\pi R9^2}\right) = \cos^2 A3 \sin 2A7$$
 (35)

The conversion factor for the forces on the cowl is:

$$(1 - (\frac{R0}{R9})^2)$$
 (36)

4. C_D and C_L

By multiplying equations (27), (28), (29), (31), (32) and (33) by equation (36), $C_{N \text{ (cowl)}}$ and $C_{C \text{ (cowl)}}$ may be determined for each case.

The coefficients of lift, C_L , and drag, C_D , for the cowl or cone are expressed in terms of the applicable value of C_C and C_N . The general equations for C_D and C_L are:

Case One:
$$C_D = C_C = 2\sin^2 A3$$
 (27a)

Case Two and Case Three:

$$C_{D} = C_{N} \sin A7 + C_{C} \cos A7 \tag{37}$$

$$C_{L} = C_{N} \cos A7 - C_{C} \sin A7 \tag{38}$$

For the cylinder:

Case One:
$$C_D = C_N = C_C = 0$$
 (39)

Case Two and Case Three:

$$c_{\text{Deyl}} = c_{\text{Neyl}} \sin A7 \tag{40}$$

$$C_{L_{cyl}} = C_{N_{cyl}} \cos A7 \tag{41}$$

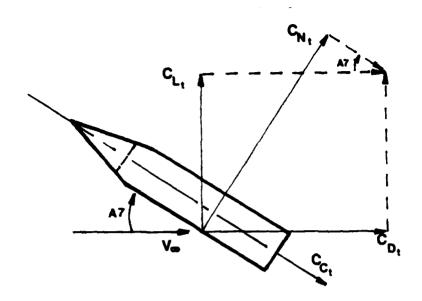


Fig. 11: AERODYNAMIC FORCE COEFFICIENTS

The total lift and drag coefficient due to the impact theory, as shown in Figure 11, is

$$c_{L_{t}} = c_{L} + c_{L_{cyl}}$$
 (42)

$$c_{D_{t}} = c_{D} + c_{D_{cyl}} \tag{43}$$

In addition to impact drag, the coefficient of skin friction drag was determined for flow over the cylinder. The equations for skin friction as a result of laminar imcompressible flow over a flat plate were applied to a cylinder of length, L [Ref. 12].

$$C_{DF} = \frac{1.328\sqrt{\mu}}{\sqrt{\rho_0 V_0} L} \tag{44}$$

This model for boundary layer was selected to provide insight concerning magnitude of skin friction. A more refined analysis using theory appropriate for hypersonic flow is needed. Equation (43) then becomes:

$$C_{D_{t}} = C_{D} + C_{D_{cv1}} + C_{DF}$$
 (43a)

B. CONTROLS

The control system on the vehicle must be capable of initiating and maintaining the required angle of attack to achieve and maintain the desired flight path angle until the vehicle is exoatmospheric. The flight path angle and velocity as the vehicle begins a vacuum trajectory will determine the apogee and the encounter geometry between the MV and the target satellite.

1. Forms of Control

There are two basic forms of control that may be used to control the vehicle, vectored thrust or aerodynamic control surfaces.

The vectored thrust approach could be achieved with external or internal reaction jets. The volume and weight

limitations of this system prevent the use of a separate engine to support the reaction jets. Therefore, the reaction jets would depend on bleed pressure from the booster. The rocket burns for only 6 seconds and the scramjet must burn most of its fuel at low altitudes for maximum efficiency. In both cases, there may be no thrust available for control while the vehicle is still subject to high dynamic pressures.

Two possible types of control surfaces are folding fins, similar to those used on the 5-inch guided projectile [Ref. 13], or storable flaps. The fins would fold at the base of the vehicle, adding to its length, and would deploy upon clearing the barrel.

The storable flap would be of the same contour as the vehicle body and would store flush with the body. The four evenly spaced flaps would be hinged on the forward edge with the rear edge elevated by an actuator. The effect would be similar to that of a variable geometry frustum. The advantage of the storable flap is that when control is not required, drag is not created by the control surface.

Any type of control surface used must be capable of withstanding the launch and up to 1,500,000 ${\rm N/m}^2$ of in flight dynamic pressure.

V. TRAJECTORY OPTIMIZATION

The gun-launched ASAT system was modeled on a HP-9830 computer. See Appendix C for the program listing. The program is designed to calculate the vehicle position, altitude, acceleration, thrust, weight, drag and lift once each time increment, t. Either the scramjet or the rocket boost vehicle described previously may be selected. Gun elevation, A, pop-up altitude, Hl, angle of attack, A7, and maximum flight path angle, A8, are input variables. Thrust, F, fuel/air ratio, F8, drag, D, and lift, L, are calculated at each time increment with the equations developed in the previous chapters. The trajectories assume a flat earth. If a maximum apogee of 1000 Km is assumed, the error between flat earth and round earth calculations is about + 5%.

A. OPTIMUM SCRAMJET TRAJECTORY

The scramjet performance is related to the dynamic pressure. If the flight path is level and at a moderately low altitude, the scramjet is theoretically capable of rather phenomenal performance. As the flight path becomes steeper, and the vehicle rapidly gains altitude, the atmospheric oxygen available for combustion decreases. Therefore, the scramjet has less time to produce useful thrust. This makes the scramjet performance sensitive to the gun elevation angle, the pop-up altitude and the angle of attack.

A trial and error method was used to determine the optimum scramjet trajectory. The gun elevation angle was varied from 15 to 45 degrees in 5 degree increments. For each gun elevation angle, the angle of attack was varied from 0 to 12 degrees in 3 degree increments. This was done for various pop-up altitudes from 500 to 11,000 meters. The results are presented in Figure 12. The maximum apogee, 558 Km, results from a gun elevation angle of 15 degrees, a pop-up altitude of 6000 meters and an angle of attack of 12 degrees.

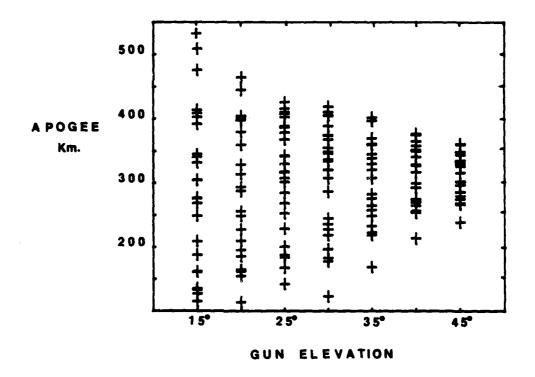


Fig. 12: SCRAMJET APOGEE AS A FUNCTION OF GUN ELEVATION FOR VARIOUS ANGLES OF ATTACK AND POP-UP ALTITUDES

The data spread indicates that as the gun elevation angle increases, the trajectory becomes less sensitive to the angle of attack and pop-up altitude. Appendix D presents the data used to produce Figure 12. Included are the angle of attack and pop-up altitude for each point.

Figures 13 and 14 represent the variation of apogee as a function of pop-up altitude and angle of attack at a given gun elevation.

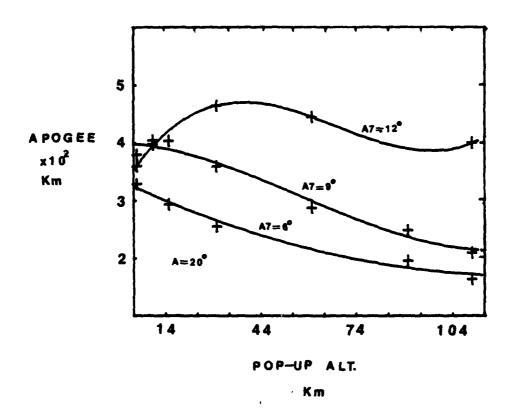


Fig. 13: SCRAMJET APOGEE AS A FUNCTION OF GUN ELEVATION, A, ANGLE OF ATTACK, A7, AND POP-UP ALTITUDE, A=20°

The A7 = 12° curve which appears in Figure 14, verifies the assumption that maximum performance for a gun elevation angle of 15 degrees and an angle of attack of 12 degrees occurs when the pop-up altitude is 6000 m.

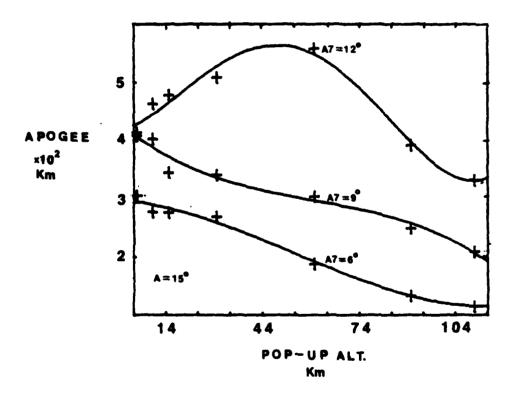


Fig. 14: SCRAMJET APOGEE AS A FUNCTION OF GUN ELEVATION, A, ANGLE OF ATTACK, A7, AND POP-UP ALTITUDE, A=15°

B. OPTIMUM ROCKET TRAJECTORY

Determination of the optimum rocket trajectory is straight forward, relative to determining the scramjet optimum trajectory. The forces affecting the rocket are thrust, drag, and gravity. Thrust is assumed constant and of a 6 second duration. Gravity varies little over the altitude range under study and is considered constant, $g = g_0$. Drag decreases with altitude. From acceleration = force/mass where force = (thrust - drag - mg) and mass decreases with time, to increase acceleration, drag must be decreased while thrust is still present. Increasing altitude as rapidly as possible is the obvious solution. Ideally the gun would be elevated to 90 degrees and the rocket fired immediately upon leaving the barrel. As a gun elevation of 90 degrees is not possible, the next best solution is to use the maximum gun elevation angle, 45 degrees, and pop-up as soon as feasible after leaving the barrel. If the pop-up altitude is 1000 m and the muzzle velocity is Mach 4.5, there are 0.7 seconds for the control system to become operative and for the rocket to ignite. The apogee achieved under these conditions is 928 Km. Table 2 is a listing of apogee as a function of popup altitude and angle of attack. The gun elevation angle is 45 degrees. Of particular interest is the first entry in Table 2. A simple rocket-boosted, 45-degree launch with no pop-up is capable of propelling the 45 Kg paylog to an altitude of 409 Km. Table 2 also shows that the apogee is insensitive to pop-up altitude up to about 2000 m.

Figure 15 represents the maximum apogee trajectory of the gun-launched scramjet ASAT. The program output for this trajectory is found in Appendix E.

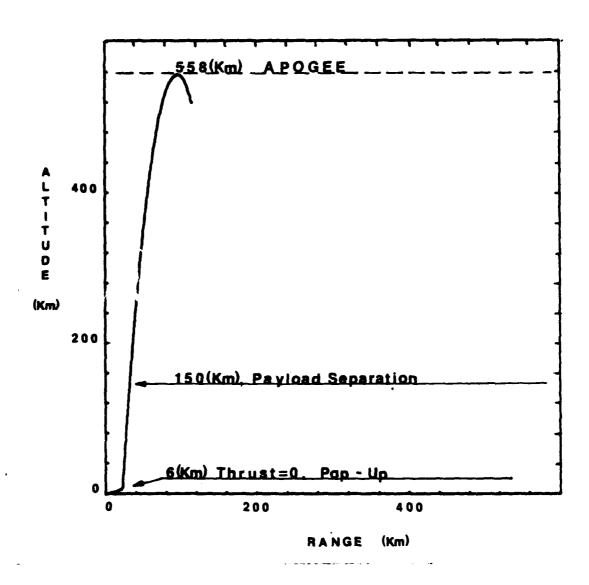


Fig. 15: SCRAMJET MAXIMUM APOGEE TRAJECTORY

TALBE II

APOGEE AS A FUNCTION OF ANGLE OF ATTACK AND POP-UP ALTITUDE FOR GUN-ELEVATION = 45°

Angle of Attack	Pop-up	Ano
	Altitude	Apogee
(DEG)	(m)	(Km)
0	0	409
3 6	100	577
6	100	753
9	100	800
12	100	928
	300	5 <i>77</i>
3 6 9	300	753
	300	800
12	300	928
3	1000	577
3 6 9	1000	753
9	1000	800
12	1000	928
3	3000	554
6	3000	716
9	3000	774
12	3000	828
	6000	531
3 6 9	6000	673
9	6000	743
12	6000	909

If a comparison is made of flight parameters at an arbitrary point, 100 Km, where the dynamic pressure can be assumed to be zero, the Mach number and flight path angle of a shot with an angle of attack of 3 degrees and a pop-up altitude of 100 - 1000 m, are 13.1 and 53.3 degrees. For the same shot with an angle of attack of 12 degrees the Mach number is 14.0 and the flight path angle is 81 degrees. By executing a 40-g pop-up, the vehicle avoids a great deal of drag and achieves greater acceleration, as previously assumed.

Figure 16 represents the maximum apogee trajectory of the gun-launched rocket ASAT. The program output for this trajectory is found in Appendix E.

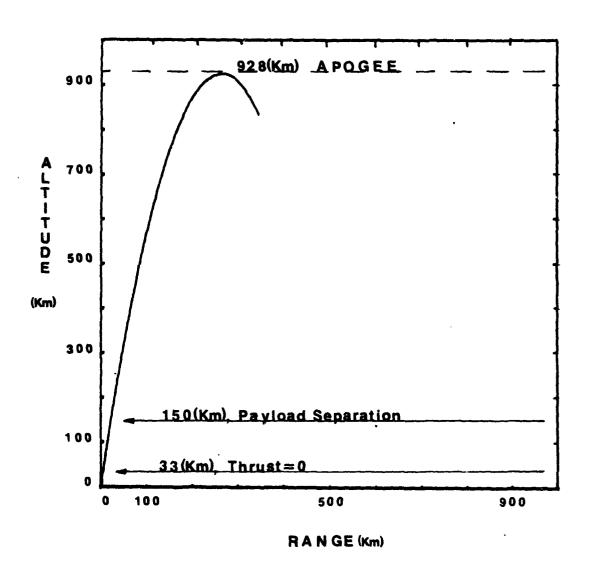


Fig. 16: ROCKET MAXIMUM APOGEE TRAJECTORY

VI. CONCLUSIONS

The design and development of a 16-inch gun-launched anti-satellite weapon is theoretically feasible. Given proper targeting information and assuming the MV can be configured for gun launching, a rocket or scramjet gun-launched vehicle can boost the ASAT payload to altitudes at which a RORSAT or EORSAT may be intercepted.

The air-breathing scramjet has a greater I sp than does the rocket; however, the scramjet thrust is altitude limited. The rocket can take advantage of a farvorable thrust-to-drag ratio at higher altitudes.

The need for an inlet on the scramjet complicates payload placement and limits the volume available for fuel. The greater density of the rocket propellent better utilizes the volume available.

The rocket boost vehicle requires few advances in design technology, and the maximum apogee of 928 Km for the rocket ASAT with same payload as the scramjet ASAT indicates that heavier payloads may be delivered by a rocket ASAT to the altitudes of interest, 250 -440 Km. The ability of the rocket boost vehicle to intercept satellites up to 409 Km, without executing a pop-up manuever, indicates that a very simple, possible spin-stabilized vehicle, can be developed to counter the low altitude threat.

APPENDIX A
PROGRAM LISTING FOR SCRAMJET THRUST

This is a listing for a TI-59 program that will, for a given altitude, calculate the thrust for a scramjet. The program executes in a closed loop, calculating the thrust for the initial Mach number, incrementing the Mach number by one and recalculating the thrust.

The memory loading prior to execution of the program:

Memory	Variable	Value	Comment
03	$^{n}{}_{d}$	0.97	
04	P ₀		Air density (1bm/in)
06	A	1.24	inlet area
07	$^{\pi}$ n	0.9	
09	^h f	18630	Btu/lbm
15	f	0.0676	
21	Δf	-0.0005	
25	\mathtt{T}_0		static air temp. (°R)
26	a ₀		sonic speed (ft/sec)

Place initial Mach number in register and press A' to execute.

```
047
                                       68 NOP
                                 048
                                       76 LBL
000
     76 LBL
                                 049
                                       17 B*-
          A
001
      11
                                       43 RCL
002
      53
           (
                                 050
                                 051
                                       21
                                            21
003
           1
      01
                                 052
                                       44 SUM
004
      85
                                 053
                                       15
                                           15
005
      93
           2
                                 054
                                       25 CLR
      02
006
          X
                                 055
                                       32 X:T
007
      65
                                       43 RCL
                                 056
      43 RCL
008
                                 057
                                       15
                                           15
          02
009
      02
                                       22
77
                                 058
                                          INV
      33 Xz
010
                                 059
                                           GE
      65
          ×
011
                                       19 D'
                                 060
           Ć
      53
012
                                            (
                                       53
013
      01
           1
                                 061
014
                                 062
                                        43 RCL
      75
กับร
      43 RCL
                                 063
                                        15
                                            15
                                        65
                                            ×
                                 064
           03
016
      03
                                            7
6
                                        07
                                 065
017
      54
           )
                                 066
                                        06
018
      54
           )
                                            9
5
019
      45 YX
                                        09
                                 067
           3
                                        05
                                  068
020
       03
                                             0
                                  069
                                        00
021
       93
022
       05
            5
                                  070
                                        85
023
                                        43 RCL
       94
          4/-
                                  071
           =
                                  072
                                             01
       95
                                        01
 024
          STO
                                  073
                                        54
                                             )
 025
       42
       13
                                  074
                                        55
                                             ÷
 026
           13
                                        53
                                             (
       68 NOP
                                  075
 027
       43 RCL
                                        01
                                             1
                                  0.76
 028
                                  077
                                        85
 029
       02
           02
                                        43 RCL
 030
                                  078
       65
           ×
 031
032
                                  079
                                             15
                                        15
       93
       07
                                  080
                                        54
                                             )
           =
                                        95
 033
       95
                                  081
                                             =
       33 X2
                                  082
                                        42
                                            STO
 034
       42 STO
                                  083
                                        08
                                             08
 035
                                        55
                                             ÷
           14
                                  084
 036
       14
                                        43 RCL
 037
       68 NOP
                                  085
       68 NOP
                                  086
                                        01
                                             01
 038
                                        95
65
 039
        68 NOP
                                  087
                                             ×
 040
        68 NOP
                                  088
                                        53
 041
        68 NOP
                                  089
  042
        68 NOP
                                  090
                                        01
                                             1
        68 NOP
                                  091
                                        85
  043
                                        93
        68 NOP
                                  092
  044
        68 NOP
                                  093
                                        02
  045
        68 NOP
                                  .094 .__65.__X
  046
```

```
32 XIT
                                      143
095
       43 RCL
                                    - 144
                                             34
                                                 LΧ
096
       14
            14
                                      145
                                             94
097
       54
            )
                                      146
                                             85
                                                   +
098
       95
            =
                                       147
                                              53
                                                   (
       55
            ÷
099
                                             02
                                                   2
                                       148
100
       53
53
                                       149
                                              93
                                              08
                                                   8
                                       150
102
       01
             1
                                      151
152
153
103
                                              65
                                                  ×
       85
                                              43 RCL
104
       01
             1
                                              14
                                                   14
105
       93
                                      154
155
156
157
158
159
                                              65
                                                  X
106
             4
       04
                                              43 RCL
107
       65
            X
                                              16
                                                   16
108
       43 RCL
                                              75
109
       14
            14
                                                    1
                                              01
110
       54
           )
111
112
113
114
                                              54
                                                   )
       33 X2
                                       160
                                              95
                                                    =
       54
            )
                                       161
                                              55
       95
            =
                                       162
163
                                              53
                                                    Ç
       42
           STO
                                              93
115
116
117
       16
            16
                                              04
                                       164
                                                    4
            <
       53
                                       165
166
                                              75
            1
       01
                                              03
                                                    3
118
       75
                                       167
                                              93
119
            4
       04
                                       168
                                                    9
                                              09
120
       93
                                                    2
                                              02
                                       169
121
122
            8
       08
                                                    X
                                       170
                                              65
       65
            -\%
                                       171
                                               43 RCL
123
       43 RCL
124
125
126
127
                                       172
                                               14
                                                    14
        16
            16
                                       173
174
                                               65
                                                    X
        65
            ×
                                               43 RCL
        43 RCL
                                        175
                                               16
                                                    16
        14
            14
                                        176
                                               54
                                                    )
 128
129
130
        54
            )
                                        177
                                                    =
                                               95
        95 =
32 X:T
                                        178
                                               34 IX
                                               32 X:T
                                        179
 131
132
133
134
135
136
137
138
139
        00
            0
                                        180
                                               01
                                                   1
        22 INV
77 GE
                                               22 INV
77 GE
                                        181
                                        182
        12
            В
                                               15
                                                    Ε
                                        183
        61 GTO
                                               61 GTO
                                        184
        00
             00
                                        185
                                               00
                                                     00
        49
              49
                                               49
                                                     49
                                        186
        91 R/S
                                               91 R/S
                                        187
        68 NOP
                                               76 LBL
                                        188
 140
        68 NOP
                                               15
                                        189
                                                   Ε
 141
        76 LBL
                                        190 32 XII.
.142
        12
            B
```

```
68 NOP
191
                                           85
                                     239
      33 X2
192
                                     240
                                            93
                                                 .
2
193
      42 STD
                                           02
                                     241
194
      17
            17
                                     242
                                            65
                                                 ×
                                           43
17
195
                                     243
                                                RCL
      61 GT0
196
      03
            03
                                     244
                                                 17
197
       78
            78
                                     245
                                            54
                                                 )
       43 RCL
                                     246
                                                 ÷
198
                                            55
199
       08
            08
                                     247
                                            53
       99 PRT
200
                                     248
                                            01
       43 RCL
201
                                     249
                                            85
       02
           02
                                     250
                                            93
                                                 2
×
202
       33 X2
203
                                     251
                                            02
       65
                                     252
204
            Х
                                            65
                                     253
                                            43 RCL
       93
205
            2+
206
       02
                                     254
                                            14
                                                 14
                                     255
256
207
       85
                                            54
                                                 )
       01
            1
208
                                            54
                                     257
258
209
       95
                                            45 YX
       42 STO
                                            03
                                                 3
210
       19
                                     259
            19
211
                                            93
212
213
                                     260
       53
             (
                                            05
                                                  5
            1
       01
                                     261
                                            54
                                                  >
214
       85
             +
                                     262
                                            95
                                                  =
215
216
                                     263
       01
            1
                                            68 NOP
       93
                                     264
                                            65
                                                 X
217
       04
             4
                                     265
                                            43 RCL
                                     266
267
268
            ×
218
       65
                                            13
                                                  13
219
       43 RCL
                                            65
                                                  Х
220
                                            43 RCL
       14
             14
221
222
223
                                     269
270
       54
             )
                                            07
                                                  07
             ÷
       55
                                            95
                                                  =
       53
                                     271
                                            45 YX
                                     272
273
274
224
225
       01
             1
                                            93
                                                 .
2
8
       85
             +
                                            02
226
       01
             1
                                            08
                                     275
276
277
278
227
228
                                            06
95
       93
                                                  6
             4
       04
229
230
       65
             Х
                                            68 NOP
       43
           RCL
                                            42
                                                STO
       17
231
             17
                                      279
                                            20
                                                 20
                                     280
232
       54
             )
                                            68 NDP
233
       95
             =
                                      281
                                            53
                                                  282
283
       65
234
             \times
                                             43 RCL
235
       53
                                             19
                                                  19
       53
236
             Ç
                                      284
                                             65
                                                  ×
237
       53
             Ç
                                             43 RCL
                                      285
238
       01
                                     286
                                             20
                                                  20
```

```
335
                                               01
       75
287
                                        336
                                               95
288
       01
             1
                                        337
                                               65
                                                     ×
289
       54
             >
                                        338
                                               43
                                                   RCL
290
       65
             X
291
292
293
                                        339
                                               04
                                                     04
       53
             Ç
                                               65
                                                     ×
                                        340
       01
             1
                                                   RCL
                                        341
                                               43
       85
                                               06
                                                     06
294
295
                                        342
       43
           RCL
                                        343
                                               65
                                                     X
       15
             15
296
297
298
299
300
                                                    RCL
                                        344
                                               43
       54
             )
       65
53
                                        345
                                               05
                                                     05
             X
                                                33
                                                    XΖ
                                        346
             (
                                        347
                                                95
                                                     =
       01
             1
                                                     ÷
3
2
                                        348
                                                55
       85
             +
                                        349
                                                03
              (
301
        53
                                        350
                                                02
302
        43
            RCL
                                        351
                                                93
             15
303
        15
                                                      1
                                        352
                                                01
        65
             ×
304
                                                      7
                                        353
                                                07
        43
            RCL
305
                                                95
                                                      =
                                        354
306
        09
             09
                                                    PRT
                                                99
                                         355
307
        65
             X
                                                61
                                         356
                                                    GTO
            RCL
        43
 308
                                         357
                                                10
                                                    E .
 309
        03
              03
                                         358
                                                76
                                                   LBL
        54
              )
 310
                                         359
                                                13
                                                      C
        55
              ÷
 311
                                                65
                                         360
                                                      X
 312
        53
              ¢
                                                53
                                                      (
                                         361
        93
 313
              .
2
3
                                         362
                                                43
                                                    RCL
 314
        02
                                         363
                                                02
                                                      02
        03
 315
                                                53
                                                    χ2
              ×
                                         364
        65
 316
                                         365
                                                65
                                                      X
            RCL
 317
        43
                                                93
              01
                                         366
        01
                                                      .
2
+
 318
                                                02
                                         367
        54
              )
 319
                                         368
369
                                                85
        54
              )
 320
                                                      1
                                                01
        55
 321
                                         370
                                                54
                                                      )
 322
         53
               Ć
                                         371
372
                                                95
                                                      =
 323
         43
             RCL
                                                99
                                                    PRT
              20
         20
 324
                                                42
                                         373
                                                     STO
 325
326
         65
              ×
                                         374
375
376
377
                                                01
                                                      01
               (
         53
                                                61
                                                     GTO
             RCL
 327
         43
                                                04
                                                      04
 328
329
         19
               19
                                                 45
                                                       45
         75
                                         378
                                                 65
                                                       X
  330
         01
               1
                                                 93
                                         379
  331
         54
               )
                                                 ÖŽ
                                                       2
                                         380
  332
         95
               =
                                                 85
                                         381
  333
         34
             ΙX
                                         382
                                                 01
  334
         75
```

```
91 R/S
                                431
383
      95
                                432
                                      68 HOP
384
      35
         1/X
                                433
                                      68 NOP
385
      65
          X
                                434
                                      68 NOP
386
      43 RCL
                                435
                                      68 NOP
387
      80
          08
                                436
                                      68 NOP
388
      95
          =
                                      76 LBL
                                437
389
      32 X:T
                                438
                                      16 A'
390
      05
          5
                                439
                                      99 PRT
391
392
      00
           0
                                      42 STO
                                440
      00
          0
                                441
                                      02
                                           02
393
      00
          0
                                442
                                      43 RCL
394
      22
         INV
                                443
                                      25
                                           25
395
      77
          GE
                                           C
                                444
                                      13
396
      17 B*
                                445
                                      25 CLR
397
      32 X:T
                                446
                                      43 RCL
398
      99 PRT
                                447
                                      02
                                           02
399
      43 RCL
                                448
                                      65
                                           X
400
      15
         15
                                449
                                       43 RCL
      99 PRT
401
                                450
                                       26
                                           26
      43 RCL
402
                                451
                                       95
                                           =
403
      17
          17
                                       42 STO
                                452
404
      34 IX
                                 453
                                      05
                                           05
405
      99 PRT
                                454
                                      99 PRT
406
      61 GTD
                                 455
                                       43 RCL
407
      01
          01
                                 456
                                       27
                                           27
408
      98
          98
                                 457
                                          STO
                                       42
409
      91 R/S
                                       15
                                           15
                                 458
410
      76 LBL
                                 459
                                           H
                                       11
411
      19 D'
                                       91
                                          R/S
                                 460
          9
412
      09
                                          RST
                                 461
                                       81
413
      09
          9
                                 462
                                       76
                                          LBL
      09
414
          9
                                463
                                       14
                                           D
          9
415
      09
                                 464
                                       65
                                           X
      99 PRT
416
                                       43 RCL
                                 465
      91 R/S
417
                                 466
                                       08
                                           08
418
      76 LBL
                                 467
                                       95
                                           =
419
      10 E.
                                       32 X1T
                                 468
420
      98 ADV
                                 469
                                       04
                                           4
421
      43 RCL
                                 470
                                       00
                                           0
422
      27
          27
                                           0
                                 471
                                       00
423
      42
         STO
                                            O
                                 472
                                       00
424
      15
          15
                                 473
                                       00
                                           0
425
      25 CLR
                                 474
                                       ממ
                                           O
426
      69 DP
                                 475
                                       00
                                            0
427
      22
           22
                                       00
                                            0
                                 476
428
      43 RCL
                                477
                                       00
                                           0
429
      02
           02
                                 478
                                      00
                                           0
430
      16 A'.
```

APPENDIX B

TI-59 SCRAMJET PROGRAM OUTPUT

Various scramjet parameters are presented for hypersonic flight at various altitudes from sea level to 150 000 feet

from sea	scramjet level to	et parameters are to 150,000 feet.		לופספוונפת זכן וואליפופסוודה דדדפוור מר א	nyperson	18777 27	ור פר אפודסת	ditous attitude
Altitude (feet)	M ₀	T _{T0}	V ₀ (ft/sec)	TS (°R)	44	Σ S	T _T 5 (°R)	T (1bf)
0	8 9 8 8 6	3112.13 4253.24 5601.83 7157.89 8921.43	5580 6696 7812 8928 10044	4051.94 4997.24 4976.24 4980.84	0.0266 0.0376 0.0396 0.0411 0.0426	1.10 1.38 1.83 2.23 2.60	5024.32 6887.59 8319.59 9913.11 11701.04	17837.82 27256.33 29712.14 31697.62 33654.02
10,000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	2898.16 3960.81 5216.68 6172.68 8308.05	5397 6476 7556 8298 9715	3761.02 4958.52 4953.15 4953.17 4967.43	0.0246 0.0371 0.0396 0.0411 0.0426	1.10 1.28 1.74 2.13	4676.10 6571.84 7949.12 9440.40	12233.47 20070.64 22165.42 23605.33 25009.45
20,000	5 6 8 9	2684.21 3668.42 4831.57 6174.68 7694.73	5187 6224 7261 8299 9336 10373	3466.42 4984.02 4992.22 4978.57 4991.95 4958.40	0.0226 0.0366 0.0401 0.0416 0.0431	1.11 1.13 1.62 2.01 2.36 2.71	4325.52 6255.82 7612.03 9000.38 10556.30	8014.64 14223.52 16136.02 17150.71 18130.12 10044.38
30,000	5 7 8 9 10	2470.20 3375.94 4446.36 5681.46 7081.25	4973 5968 6963 7957 8952 9947	3309.85 4743.11 4991.60 4959.58 4972.51 4989.23	0.0211 0.0341 0.0401 0.0416 0.0431	1.03 1.06 1.50 1.90 2.24	4009.25 5802.09 7241.67 8527.83 9968.16	5235.26 9245.33 11322.25 12014.92 12677.54

$\begin{array}{ccc} & & & & & & & & & & & & & & & & & &$	11 3774.17 3177.28 07 5491.71 5693.92 44 6982.58 7345.04 82 8240.16 7896.57 16 9610.14 8323.30	11 3774.17 1958.56 07 5491.71 3509.87 44 6982.58 4527.66 82 8240.16 4867.64 16 9610.14 5130.69 48 11125.52 5384.73	11 3774.17 1215.46 07 5491.71 2178.20 44 6982.58 2809.83 82 8240.16 3020.81 16 9610.14 3184.06	11 3774.17 464.24 07 5491.71 831.95 44 6982.58 1073.90 82 8240.16 1153.78 16 9610.14 1216.13	12 4055.55 182.82 08 5898.92 328.61 52 7323.49 396.20 92 8632.22 420.59 27 10098.09 443.96
χ Σ			.4.4.4.	2.1.1.	
44	0.0196 0.0321 0.0396 0.0416 0.0431	0.0196 0.0321 0.0396 0.0416 0.0431	0.0196 0.0321 0.0396 0.0416 0.0431	0.0196 0.0321 0.0396 0.0416	0.0211 0.0346 0.0401 0.0416
T _S	3032.62 4473.08 4942.83 4951.35	3023.62 4473.08 4942.83 4951.35 4962.45	3032.62 4473.08 4942.83 4951.35	3032.62 4473.08 4942.83 4951.35	3247.16 4775.08 4990.11 4963.27 4976.52
v_0 (ft/sec)	4843 5811 6780 7748 8717	4840 5808 6777 7745 8713 9681	4840 5808 6776 7744	4840 5808 6776 7744 8712	5025 6030 7035 8040 9045
T _{TO}	2339.93 3197.90 4211.87 5381.83 6707.79	2339.93 3197.90 4211.87 5381.83 6707.79	2339.93 3197.90 4211.87 5381.98 6707.79	2339.93 3197.90 4211.87 5381,83 6707.79	2517.48 3440.56 4531.46 5790.20 7216.78
Σ ^O	200	5 7 8 9 10	2 9 2 8 9	98765	296769
Altitude (feet)	40,000	20,000	000,09	80,000	100,000

Altitude M_0 (feet)	T _{TO}	V ₀ (ft/sec)	T _S (°R)	44	Σ S	T _T 5 (°R)	T (1bf)
	3011.26 4115.38 5420.26 6925.89 8632.27	5490 6588 7686 8784 9882 10980	3902.20 4941.18 4964.63 4967.47 4980.29	0.0256 0.0371 0.0396 0.0411 0.0426	1.11 1.34 1.79 2.18 2.54 2.90	4856.84 6720.88 8144.94 9690.26 11423.69 13344.40	24.72 38.81 42.91 45.74 48.52 51.31

APPENDIX C GUN-LAUNCHED SCRAMJET/ROCKET ASAT MISSION PROFILE, PROGRAM LISTING

```
1 REM THIS PROGRAM WILL CALCULATE THE FLIGHT PATH FOR A 16", GUN-LAUNCHED ROCKET 2 REM OR SCRAMJET VEHICLE FOR USE IN AN ANTI-SATELLITE MISSION. FLAT EARTH 3 REM TRAJECTORY IS ASSUNED. 4 REM FOR A SINGLE RUN WITH OUTPUT EVERY 10 SECONDS, ENTER RUN. 5 REM FOR A PROGRAM THAT WILL CALCULATE APOGEE FOR GUN ELEVATON ANGLES, (15-45) 6 REM DEG, ANGLE OF ATTACK, (0-12) DEG., AND POP-UP ALTITUDE, (100-11500) METERS, 7 REM RUN, DRAW THE AXISES THEN CONTINUE AT LINE 20.
                                                                                                                                               APOGEE RUN W8=@(SCRAMJET), W8=1(ROCKET).
                                                                                                                                                                                                                                                                                                                                                                                                             --BXIZIS SIXH-
                                                                                                                                                                                                                                                                       2180
                                                                                                                                               --FOR
                                                                                                                                                                                                                                                                                                              IF 87<15 THEN 450
                                                                                                                                                                                                                                                                      100 IF H1>11500 THEN
                                                                                                                                                                                                                                                                                                                                                      IF A>10 THEN 450
A4=A=45
                                                                                                                                                                                                                                                                                                                                                                                                                         X9=66666.667
                                                                                                                                                                                                                                                                                                                                                                                                                                      79=66666.667
                                                                                                                                                                                                                                                                                                                                          R=84=84-5
                                                                                                                                                                                                                                            H1=H1+166
                                                                                                                                 G010 200
                                                                                                                                                                                                                                                                                                                                                                                             G010 88
                                                                                                                                                                                                                                                                                   H7=H7+3
                                                                                                                                                                                                                84=8=45
69=8
                                                                                                                                                                                                                                                                                                R=R4
                                                                                                                                                                                                                                                                                                                           A7=3
                                                                                                                                                                                                                                                                                                                                                                                 H7=0
                                                                                                                                                                                       A7=-3
                                                                                                                                                                                                    H1=0
                                                                                                                                                             Ø=8M
                                                                                                                                                                          M9=1
                                                                                                                                                                                                                                                                                                10
                                                                                                                                 4
8
8
8
8
8
8
8
                                                                                                                                                                                                   000000
000000
```

```
...
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          "ROCKET (INPUT(1)); SCRAMJET (INPUT(0))"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            --PROGRAM INITIALIZATIION-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            INPUT HI
DISP "INPUT ANGLE OF ATTACK (DEG).";
            "HAVE THE AKES BEEN DRAWN?"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      INPUT A
DISP "INPUT POP-UP ALT(M)";
                                                                                                                                                                                                                                                                                                                                                       XAXIS 0, X9/10,0, 3*X9
YAXIS 0, Y9/10,0, 3*Y9
                                                                                                                                                                                                                                                                                                   SCALE 0,3*X9,0,3*Y9
                                                                                                                 DISP "YES=1,N0=0";
                                                                                                                                                                             INPUT 28
IF 28=1 THEN 450
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                A8=80
M3=45
FORMAT 5F14.3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               R9=0.4572
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              WAIT 160
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           WAIT 188
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     WAIT 188
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              INPUT A7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            INPUT W8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        REM
PRINT
PRINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PRINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      PRINT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             69=10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           A3=10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         N9=01
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                18=3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ± 0×
20 = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1 = 8×
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  )<u>...</u>(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  T=1
DEG
        ^{\prime\prime} ^{\prime\prime
```

```
PRINT "ELEVATION ANGLE=";A"POP-UP ALT=";H;
PRINT "ANGLE OF ATTACK=";A7"FUEL(KG)=";M3
PRINT "MAXF,P,ANGLE=";A8" DELTA TIME=";T
PRINT "INLET AREA(M+2)=";A0
                                                                                                                                  IF W8>0 THEN 2200
IF W9=1 THEN 850
DISP "WANT PRINT OF INPUT YES=1 NO=0";
                                                                                                                     PLOT X2,Y2
IF W9=1 THEN 1888
                                                                                                                                                            F W7<1 THEN 850
                                                           R7=1-(R8/R9)+2
                                                                                                                                                                                                                <2=X3=X1+U*T
                                                                                                                                                                                                                       72=73=71+4*1
                                                                                                                                                                                                    U8=V1*COSA
                                                                                                                                                                                             V8=V1*SINA
                                                                                                                                                                                                          PLOT X1, Y1
                                                                                                 G=9.807
U=V1*COSA
                                       89=8.1297
88=8.8993
88=8.3556
                                                                               G1=1.4
R=1.22642
H=7620
                                                                                                                HNIS*IAH
                   M2=M=4.5
                                V1=M2*A2
                                                                                                                                                      INPUT WZ
                         A2=368
                                                                 M1=325
      71=78
8X=1×
                                                                        46=M1
             M7=10
                                                                                                                                                                                                                             T1=T
\mathbf{c}
```

**************************************	: 	
1 2444	* Z*), MACH #(M)
**************************************	LIFT VELOCITY MASS **********************************	W W2)/T Y2)/T Y2)/T FLIGHT PRTH RNGLE(R9), DYN.PRESS.(Q1), MACH #(M) (Y3-Y2)/(X3-X2)) (Y3-Y2)/(X3-X2)) Y3-Y2)/(K2+U12)*EXP(-Y3/H) W8)
**************************************	LIFT VELOCITY ************************************	.ST ITH ANGLE(A9), (-?3/H)
OUTPUT FORMAT *********************************	**************************************	T
00 PRINT ** 00 PRINT ** 00 PRINT :*	PRINT	100 M7=M7+ 110 M6=M1- 120 M3=M3- 140 W=CX3- 150 IF CY3- 150 MF CY3

```
REM------IF MORE THAN 1 KG. OF FUEL CALL SCRAMJET THRUST ROUTINE
IF M3>1 THEN 2600
                                                                                                                                                                                 CONT AT SONIC SPEED ROUTINE-----
                                                                                                                                                                                                                           IF Y3>10970 THEN 1550
REM-----FUEL FLOW ROUTINE FOR SCRAMJET
                                                                                                                                                                                ----IF VEHICLE IS ROCKET
                                                                                                       WRITE (15,510)T1,M,D,A,F
WRITE (15,510)L,V2,M6,Q1,Y3
                                                                                                                                                                                                                                           IF M>6 THEN 1530
F8=0.0226+0.011*(M-5)
GOTO 1580
F8=0.037+0.00177*(M-6)
GOTO 1580
        F ¥9≈0 THEN 1240
F Y3>100000 THEN 1380
                                                                                                                                                                                                                                                                                        IF M>7 THEN 1530
F8=0.021+0.0093*(M-5)
GOTO 1580
                                                                                                                                                                                       IF M8>0 THEN 1580
                                                                     F J2=0 THEN 1388
                                                                                                IF W9=1 THEN 1750
                                   F J=1 TH5N 1300
F J=5 THEN 1300
                                                                                                                                    IF W9=1 THEN 90
                                                                                        V2=SQR(U+2+V+2)
                                                    11=INT(J/10)
                                                              (2=(J/10)-J1
                           5070 1360
                                                                               GOTO 1360
                                                                                                                                                                       2=73
                                                                                                                                                              SX=XX
                                                                                                                                             X1 \pm X2
                                                                                                                                                      Y1=Y2
398
                                                                                                                                                                               2000000
2004000
200000
```

		1	
		THL"	:
	! ! !	<81 <81	
- (3 8 6) -	 	6, EL	
A FUNCTION OF ALT.(M/SEC)	-SRCAMJET CONDIION POST FUEL EXHAUSTION-	OUTPUT FOR APOGEE PROGRAM MODE	
SOUND AS A	CONDTION P	OR APOGEE P	S-
REM	3556 9.3556 98 98 88 1-(RØ/R9)↑ 1896	73+(V+2/ 59=1 THEN 71 " 71 "TR.AL	
20000000000000000000000000000000000000	6000000000000000000000000000000000000	くてくてかり 45000000	ათადიდიდად გ⊶ოც4ოები

```
GOTO 2020
P8=0.01745*ATN(TANA3/(SQR((TANA7)+2-(TANA3)+2))
L2=(COSA3)+2*SIN(2*A7)*((P8+1.57)/3.14)+0.0161*COS(P8*57.29578)
L2=L2*((COSA7/SINA7)*TANA3+2*TANA7*(COSA3/SINA3))
                                                                                                                            L3=((P8+1.57)/3.14)*(2*(SINA3)†2+(SINA7)†2*(1-3*(SINA3)†2))
L3=L3+0.2387*C0S(P8*57.29578)*SIN(2*A7)*SIN(2*A3)
L3=L3*R7
                                                             .3=(R7*(2*(SINR3)+2+(SINR7)+2*(1-3*(SINR3)+2)))
  -HYPERSONIC AERODYNAMICS--
                                                                                                                                                                                                L7=1.69765*(L9/R9)*(SINR7)*2*COSR7
L8=1.69765*(L9/R9)*(SINR7)*2*SINR7
GOTO 2090
L5=R7*2*(SINR3)*2
                                                 .2=R7*(C0SA)+2*SIN(2*A7)
                                                                                                                                                                         5=L2*SINA7+L3*C0SA7
                                                                                                                                                                                      _6=L2*C0SA7-L3*SINA7
            Y3<H1 THEN 2070
                       IF 8588 THEN 2070
IF 87583 THEN 1950
                                                                                                                                                                                                                                                                                                              0=Q1*H9*C+D6
                                                                                                                                                                                                                                                16=L7=L8=0
                                                                                                                                                                                                                                                                                       -=C6*A9*@1
                                                                                                                                                                                                                                                                                                  GOTO 2430
                                                                                                                                                                                                                                                                                                                                     GOTO 1010
                                                                                                                                                                                                                                                                           C6=L6+L7
                                                                                                                                                                                                                                                             C=L5+L8
                                                                                                                                                                                                                                                                                                                           02=0
200800
200800
201800
201100
201100
201100
201100
201100
                                                                                                                                                                                                                         2060
```

	HEN 2370	
.IZATION	IN POST FUE	SEPARATIO
INITIAL	. CONBITC	. PAYLOAI 190
	i	
REM	1 E C C C C C C C C C C C C C C C C C C	73<1 38 0 18
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	. 4 N 0 V 0 V	0.444 0.0040

```
F=(1450-(Y3-3048)*0.1696)*(M-7)+21000-2.034*(Y3-3804)
                                                                                                                                                                                                    PRINT "FALLING OUT OF SKY";" ALT="; Y3"RNG="; X3"A="A
PRINT "GUN.EL="A4,"ALFA="A7,"TALT="H]
                                                                                                                                                                                                                                                                                                                                                                      IF Y3>6096 THEN 2780
IF M>6 THEN 2730
F=(7800-(Y3-3048)*0.5249)*(M-5)+12200-1.4*(Y3-3048)
                                                                                                                                                                                                                                                                                                                                                                                                                        IF M >= 7 THEN 2760
F=(2100-(Y3-3048)*0.0656)*(M-6)+18800-1.9*(Y3-3804)
                                                                                                            GOTO 2530
U9=1.336E-06
C7=1.328/SQR((EXP(-Y3/H)*(M*A2)*L9)/U9)
D6=01*6.283*(R9/2)*L9*C7
IF L=0 THEN 2560
                                                                                                                                                                                                                                                                                 '=(9500-Y3*0.5577)*(M-5)+17800-1.837*Y3
                                                                                                                                                                                                                                                                                                                                             F=(2133-Y3*0.2241)*(M-7)+29700-2.49*Y3
                                                                                                 U9=((Y3-25000)/-3.873E+09)+1.422E-05
                                                                                                                                                                                         REM------RPOGEE FRULT------
-SKIN FRICTION DRAG-
                                                                                                                                                                                                                                          REM--------SCRAMJET THRUST IF Y3>3048 THEN 2690
                      U9=(Y3/-2,997E+09)+1.789E-05
GOTO 2530
                                                                                                                                                                                                                                                                                                                    F=2133*(M-6)+27388-2.395*Y3
         F Y3>11000 THEN 2460
                                                                                     F Y3>75000 THEN 2520
                                                F Y3>25000 THEN 2490
                                                                                                                                                                                                                                                                   F M>6 THEN 2648
                                                                                                                                                                                                                                                                                           GOTO 3100
IF M>2 THEN 2620
                                                             U9=1.422E-05
                                                                                                                                                                                                                                                                                                                                                           G010 3188
                                                                                                                                                                                                                                                                                                                                                                                                              GOTO 3100
                                                                                                                                                                            6070 2130
                                                                                                                                                                                                                                                                                                                                  GOTO 3100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GOTO 3100
                                                                                                                                                                                                                              GOTO 98
           2442
2443
2448
2448
6034
6034
                                                            2470
2480
2490
2500
                                                                                                                          2698
                                                                                                                                                                                                                                                                                                                                                                                                            2720
                                                                                                                                                                                                                                                                                                                                                                                                                                     2740
2750
                                                                                                              5518
                                                                                                                                                                                                                                                                                                                                              2670
                                                                                                                                                                                                                                                                                                                                                           2680
```

```
F=(1600-(Y3-12192)*0.19685)*(M-6)+5700-0.72178*(Y3-12192)
                                                                                                                                                                                                                                                                                                                                                                         ÷(2500-(Y3-12192)*0.3281)*(M-5)+3200-0.3937*(Y3-12192)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     F=(500-(Y3-12192)*0.0164)*(M-7)+7300-0.9186*(Y3-12192)
                                  =(6200-(Y3-6096)*0.72178)*(M-5)+8000-0.919*(Y3-6096)
                                                                                        F=(1900-(Y3-6096)*0.06562)*(M-6)+14200-1.64*(Y3-6096)
                                                                                                                                                                                                     F=(4000-(Y3-9144)*0.4921)*(M-5)+5200-0.656*(Y3-9144)
GOTO 3100
IF M >= 7 THEN 2940
F=(2100-(Y3-9144)*0.164)*(M-6)+9900-1.4*(Y3-9144)
                                                                                                                            F=(933-(Y3-6096)*0.08737)*(M-7)+16100-1.57*(Y3-6096)
                                                                                                                                                                                                                                                                                                F=666.7*(M-7)+11388-1.31*(Y3-9144)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            F=(17800+9500*(M-5))*EXP(-Y3/H)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             F=(27300+2133*(M-6))*EXP(-Y3/H)
                                                                                                                                                                F Y3>12192 THEN 2960
F M>6 THEN 2910
                                                                                                                                                                                                                                                                                                                                    F Y3>15240 THEN 3050
F M>6 THEN 3000
73>9144 THEN 2870
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     F=4.45*F*(A0/0.111)
GOTO 1490
                   MY6 THEN 2820
                                                   GOTO 3100
IF M>7 THEN 2850
                                                                                                                                                                                                                                                                                                                                                                                           GOTO 3100
IF M>2 THEN 3030
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      F M>6 THEN 3080
                                                                                                                                               GOTO 3188
                                                                                                                                                                                                                                                                                                                                                                                                                                               GOTO 3100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       GOTO 3166
                                                                                                                                                                                                                                                                              GOTO 3100
                                                                                                                                                                                                                                                                                                                   GOTO 3100
                                                                                                                                                                 2870
                                                                                                                                                                                   2880
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    3838
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           3868
                                                                                                                                                                                                                         2900
                                                                                                                                                                                                                                                                                                                                                                                                                                3010
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       3840
3850
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3888
```

APPENDIX D

GUN-LAUNCHED SCRAMJET ASAT APOGEE AS A FUNCTION OF GUN ELEVATION, ANGLE OF ATTACK AND POP-UP ALTITUDE

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
30 35 40 45	0 0 0 0	0 0 0 0	123 169 214 239
15 20 25 30 35 40 45	3 3 3 3 3 3	500 500 500 500 500 500	162 186 209 236 265 275 286
15 20 25 30 35 40 45	. 3 3 3 3 3 3 3	1000 1000 1000 1000 1000 1000	161 165 208 228 258 275 302
15 20 25 30 35 40 45	3 3 3 3 3 3	1500 1500 1500 1500 1500 1500	135 162 188 228 258 272 282
15 20 25 30 35 40 45	3 3 3 3 3 3	3000 3000 3000 3000 3000 3000	127 155 184 219 249 270 280

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
25 30 35 40 45	3 3 3 3	6000 6000 6000 6000	168 197 233 265 274
20 25 30 35 40 45	3 3 3 3 3	9000 9000 9000 9000 9000	114 157 183 223 257 269
25 30 35 40 45	3 3 3 3	11000 11000 11000 11000 11000	142 178 219 254 267
15 20 25 30 35 40 45	6 6 6 6 6	500 500 500 500 500 500	305 329 343 334 330 328 329
15 20 25 30 35 40 45	6 6 6 6 6	1000 1000 1000 1000 1000 1000	227 314 330 337 332 328 329
15 20 25 30 35 40 45	6 6 6 6 6 6	1500 1500 1500 1500 1500 1500	276 294 318 337 332 329 326

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
15 20 25 30 35 40 45	6 6 6 6 6 6	3000 3000 3000 3000 3000 3000	269 256 302 321 331 327 326
15 20 25 30 35 40 45	6 6 6 6 6	6000 6000 6000 6000 6000 6000	188 228 253 287 308 317 316
15 20 25 30 35 40 45	6 6 6 6 6 6	9000 9000 9000 9000 9000 9000	133 196 229 321 283 300 303
15 20 25 30 35 40 45	6 6 6 6 6	11000 11000 11000 11000 11000 11000	115 164 201 245 272 293 297
15 20 25 30 35 40 45	9 9 9 9	500 500 500 500 500 500	409 380 368 355 345 341 333

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
15 20 25 30 35 40 45	9 9 9 9 9	1000 1000 1000 1000 1000 1000	403 405 387 374 362 360 333
15 20 25 30 35 40 45	9 9 9 9	1500 1500 1500 1500 1500 1500	345 404 403 374 360 350 344
15 20 25 30 35 40 45	9 9 9 9 9	3000 3000 3000 3000 3000 3000	341 360 389 389 370 358 348
15 20 25 30 35 40 45	9 9 9 9	6000 6000 6000 6000 6000 6000	304 288 342 368 361 358 349
15 20 25 30 35 40 45	9 9 9 9 9	9000 9000 9000 9000 9000 9000	249 249 285 321 339 341 332

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
15 20 25 30 35 40 45	9 9 9 9 9	11000 11000 11000 11000 11000 11000	209 210 269 308 321 330 325
15 20 25 30 35 40	12 12 12 12 12 12	500 500 500 500 500 500	414 360 317 346 339 293 335
15 20 25 30 35 40	12 12 12 12 12 12	1000 1000 1000 1000 1000 1000	463 398 379 349 361 293 335
15 20 25 30 35 40 45	12 12 12 12 12 12	1500 1500 1500 1500 1500 1500	478 479 408 349 361 352 337
15 20 25 30 35 40 45	12 12 12 12 12 12 12	3000 3000 3000 3000 3000 3000	509 465 439 411 372 365 355

Gun Elevation (DEG)	Angle of Attack (DEG)	Pop-up Altitude (m)	Apogee (Km)
15	12	6000	558
20	12	6000	445
25	12	6000	426
30	12	6000	405
35	12	6000	402
40	12	6000	375
45	12	6000	361
15	12	9000	392
20	12	9000	442
25	12	9000	416
30	12	9000	419
35	12	9000	405
40	12	9000	379
45	12	9000	360
15	12	11000	332
20	12	11000	401
25	12	11000	411
30	12	11000	406
35	12	11000	397
40	12	11000	377
45	12	11000	360

APPENDIX E

MAXIMUM APOGEE TRAJECTORY, LISTINGS

Units:

Time = Seconds
Velocity = Meters/Second
Lift
Drag
Thrust
Mass = KG
Altitude = Meters
Dynamic = Newton/Meter
Pressure
Angle = Degrees

SCRAMJET

49344.343 894.279 THRUST 15.724 1668181.437 DYN PRESS 5546.445 321.831 POP-UP ALT≕ 6000 FUEL(KG)= 45 DELTA TIME= 1 4.895 1749.846 VELOCITY ELEVATION ANGLE= 15 PC ANGLE OF ATTACK= 12 FU MAXF.P.ANGLE= 80 DEL7 INLET AREA(M†2)= 0.0993 2. ପ୍ରସ୍ତ ଓ. ପ୍ରସ୍ତ

(. 2. 626.	136.64 297.92		 88628.689 3749.368
* ⊶ [∿ :	* 1-	* 4 00	**** **** ****************************	***** 0.000 13274.794
* → © > * • • • >	* • • • • • • • • • • • • • • • • • • •	* একে:	* 07: * 08: * 08: * 08: * 08:	
k ~ ω ⊗ ×	* (10) >	* 10 00 * * 00 00 * * ^- *	* 4 C () * O () ()	
41.666	K UU A	k のの k k のの k k する k k かんす k	* 10 d : * 10 d : * 20 d : * 20 (0 :	***** 0.000 106870.276
**************************************	k 100 ak	**************************************	* * * * * * * * * * * * * * * * * * *	
	((C)	ගිනි		
× (Ω +	K WA	* = = ×	* 50 00 : * 00 00 : * 40 00 :	***** 0.000 191628.634
	K UNA K UNA	* • • • *	**************************************	
* (2)	ः एकताः चित्र		* ታወ ጣ * * ውወ »	k 📆
	e gera e (Ora)	୍ୟ ପ୍ର	k 4 ② ; k ゲ ② ; k ゲ ② ;	k (D)
	6 Q *	* (2)(2) *	**************************************	ak eT\ ak
— @ > . @ @ >	(N)	୍ଷ୍ଟ ଓଡ଼ିଆ	ং ক হা ং ক <u>হা</u> ং ক <u>হা</u>	k 🛶 🤉

жээхэхжжээх 101, Б ББ	н 100 г К — 1 К 100 Г К	. * * * * * * * * * * * * * * * * * * *	******* 84. BSB	æ,
***********	* *	****************	************************	334666.261
୍ଷର	വെച വെയ	ඔ@ ඔ@	. ഗമ ഗമം	 855 8 73. 4 15
**************************************	* (P) (D) * · · · * (D) ++ ·	**************************************	* (7)	* 4 4 00 00
**************************************	* IO (7) :	**************************************	* * * * * * * * * * * * * * * * * * *	***** 6.000 392945.624
**************************************	*	**************************************	* (10) * • • • • • • • • • • • • • • • • • • •	***** 6.666 416416.678
× → Θ : × • • : × • • Θ : :	Հա յ ա «	**************************************	* * * * * * * * * * * * * * * * * * *	+ :
k — (2) ×	K (1)で x K (1)で x K (1)で x	* ඔබ: * ඔබ: * ඔබ:	* * * 000: * 100: * 1-00:	
k ©D = H k OJ = H	K 00 00 8	**************************************	** ** ** ** ** ** ** ** ** **	* in:
11. 11. 10. 10. 10. 10. 10. 10. 10. 10.	к 40 0 к к 1 1 1 1 1 к 1 1 1 1 1 1 1 1 1 1 1 1	n 1777 d	* @ @ . * * * *	* 17: * 17:
* (D) *	K OHO X K OH OX K OH X K OH X	* ପ୍ରତ * • • • • •	* * * \$ \$ \$ \$ * \$ \$ \$ \$ * \$ \$ \$ \$ * \$ \$ \$ \$	* 00 :
ඔබ ම	လေးကြား ကြောက် ကြောက် ကြောက်	* * * * * * * * * * * * * * * * * * *	**************************************	***** 0.666 494666.364

241,866 6,666	3,226 1639,875	කුව.	77.872	6.666 585286.458
**************************************	** ** ** ** ** ** ** ** ** ** ** ** **	**************************************	* : * W© :	***** 6.000 514825,912
**************************************	* * * * * * * * * * * * *	****************	* * * * * * * * * * * * *	k (Mi≥
40 (A)	k 4 € × k 0 00 × k 0 00 ×	***********************	**************************************	***** 6.696 531122.721
* 00 : * 01 : * :	(* * * ?	****************	**************************************	***** 6.000 537800.075
* (V) 3 	* που * που * που	**************************************	k • • ≥ k (~ ⊙ ≥ k (0 ≥ k (0 ≥	k ਦੇ: k 10: k ×
************ 301.000 6.000 8.000	k - √ × k - √ 0 k - 0 k	**************************************	* • • * * (1) (2) (4) * (2) (4) * (3) (4) * (4) (4)	k 寸 3
K	k ← 60 k ← 6	**************************************	к (() — » к — » к — »	****** 0.000 551947.938
**************************************	**************************************	k 3	** ** ** ** ** ** ** ** ** **	k in x
א ניו א	k Substantial	K	**************************************	k UD: k UD:
	है । हिंदी हिंदी हिंदी हिंदी	K (20 (20)	**************************************	k tij a
	7. 188 27. 188 188	്മാമാ	5 50 50 c	k ហ៊ុះ k ហ៊ុះ

* * * * * * * * * * * * * * * * * * *	k (1): k (1): k : k (2): k (2): k (2):	* 10 ፡ * 10 ፡ * ፡ * ፡ * ፡	k (1): k k k	* 寸: * 0: * *	* (7): * 17): * : * : * :	k (V): k iO: k : k :	********** .554 .888 528276.398 .********
**************************************	K 1 9 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	## (F) H H H H H H H H H H H H H H H H H H H	k 40 3 k 1 3 k 3 k 3 k 3 k 3 k 3 k 3	* : : : : : : : : : : : : : : : : : : :	* 3 * 2 * 2 * 3 * 4 * 3 * 4 * 3	k 3 k 3 k 3 k 3 k 3 k 3	**************************************
 < 0.00 < 0.0	1.855. 1.855. 30.751. 88.751.		6 3 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	K 3 K 3 K 3 K 3 K 3 K 3 K 3 K 3 K 3 K 3	**************************************		k 34 k 34 k 34 k 34 k 34
361.000 6.000 8.600	: ;4 : ;4	381.888 8.888		k a	411.866	421.666	* ** * ** * ** * ** * **

					*****	ANGLE	
II. ROCKET	: 1ଡଡ	216			******	DRAG	
	FOP-UP ALT= 188	FUEL(KG) = 2	DELTA TIME= 1		*****	MHCH	
	ELEVATION ANGLE= 45	ANGLE OF ATTACK= 12	MAXF.P.ANGLE= 80	INLET AREA(M+2)= 0	************************************	ELAPSED	

_	⊢	88 88 88	386 293	888 438	988 147	ଉ .ଜ ନ୍ଧ	9.000 4.751	996 731	ଓ .ଉ ଉଟ ଓ.ଉଉ1	666 571
- 00 AH-	18 ::	**** 84576.000 2804.000	***** 84556.3 12733.3	****** 9.000 32979.430 ******	< r⊸⇒	* 41.9 00.	*** 15427 **	6.000 192736.731 ******	ကာတွ	ებ. დდ.
	DYN PRES	**************************************	* 4:00 * 00 * 00 * 00 * 00 * 00 * 00 * 00	**************************************	: : : : : : : : : : : : : : : : : : :	**************************************	r 11	81.018 81.018 6.090	88.784 8.688 8.688	
5000	SOUTH	i	45000 046 1500 066	**************************************	100 x	k :#	c ;∳ c ;∳		* * 66 * 66 * 66 *	
	VELOCITY	k 34 k 34 k 34	* 100 × * 100 × * 100 ×	* * * * * * * * * * * * * * * * * * *	オロシ	**************************************	13.687 3946.168 *********	**************************************	* * * *	12.60 655.66
A TO SEE THE S	. 취 취 기 기 기 기 기 기 기 기 기 기 기 기 기 기 기 기 기 기	******** 2.000 89467.605 ********	୍ ଓଡ଼ିଆ ଜନ୍ମ	**************************************	CU 34 34 34 34 34 34	**************************************	41.888 41.888 8.888 ****************************	**************************************	61.000 8.000 **********	71.686

651982.276	674753.046 674753.046 **** 696543.115	***** 717352.485 **** 0.000 737181.155	756829. (25 ***** # ###	773896.394 **** 0.000 790782.964	* * * * * * * * * * * * * * * * * * *	**** 835558.473 **** 8.85558.473 **** 8.8666
* * * * * * * * * * * * * * * * * * *	**************************************	**************************************	: ; ∳:	* *	¢ :#k	* * * * * * * * * * * * * * * * * * *
	**************************************	** **	6.666 8.666 8.**************************	******** 36.666 ****** 6.666 36.666 *****	**************************************	** ** ** ** ** ** ** ** ** ** ** ** **
2487.237	2312.462 ************************************	**************************************	1936.287 1936.287 ************************************	1843.311 ******** 6.838 1758.691 *******	1659.721 ************************************	**************************************
र्व अ च अ च अ	11.000 ******** 21.000 6.000	(- 0 * - 0 * * 0 0 * 0 0 *	20 CD * CD	6.000 **********************************	* * * * * * * * * * * * * * * * * * *	**************************************

. *** *** *** *** *** *** *** *** *** *	321, 666	トの4・4	ର ପ୍ରଧାନ	62.400	
331.000 0.000 0.055 341.000 0.000 0.055 341.000 0.000 0.000 341.000 0.000 0.000 341.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 0.000 351.000 0.000 351.000 <	3	1301.260	39,666	ପ୍ରତ୍ର ପ୍ରତ୍ର	0505.
331.000	*****	***********************	*********	********	水水水水水
6.000 1215.120 30.000 871507. 341.000 3.900 9.000 871529. 9.000 341.000 1130.924 9.000 875.053 9.05 9.000 1130.924 9.000 875.053 9.05 8.000 1049.141 3.518 9.000 895.70 8.000 1049.141 3.518 9.000 895.70 8.000 970.382 30.000 9.000 895.87 8.000 970.382 30.000 9.000 9.05 8.000 895.445 30.000 47.84 8.86 8.000 895.445 30.000 47.84 8.84 8.000 895.445 30.000 9.000 9.057 8.000 895.445 30.000 9.000 9.050 8.000 895.445 30.000 9.000 9.000 8.000 895.445 30.000 9.000 9.000 8.000 895.445 30.000 9.000 9.000 8.000 895.846 9.000 9.000 9.000 <	331,000	4,198	ପ୍ରପ୍ର ପ	68,359	
**************************************	ପ୍ରତିଷ୍ଟ ପ	1215.120	36,666	ପ୍ରତ୍ର ପ	1507.
341.800	****	***************	·***********	**	****
8.000 881529. 8.000 881529. 8.100 8.000 8.000 8.000 <t< th=""><th>341.000</th><th>99.0 9</th><th>ପ୍ରପ୍ରତ</th><th>r.</th><th>999.9</th></t<>	341.000	99.0 9	ପ୍ରପ୍ରତ	r.	99 9. 9
**************************************	ଉପ୍ରତି ଓ	1130.924	36.666	ର ଓଡ଼େ	500
351,000 3.618 0.000 55.053 0.000 48,000 1049.141 30.000 6.000 890570. 361,000 970.382 30.000 0.000 898630. 48,888 88,000 47.845 898630. 571,000 895.445 30.000 47.845 888 89.000 47.845 89.000 895.445 30.000 47.845 896.000 895.445 89.000 89.000 895.445 88.000 47.845 895.445 89.000 89.000 99.000 895.458 89.000 89.000 91.899. 896.000 89.000 89.000 91.000 886.000 89.000 89.000 92.000 888.888 89.000 89.000 92.000 888.888 89.000 89.000 92.000 888.888 89.000 89.000 92.000 888.888 89.000 89.000 92.000 888.888 89.000 92.000 92.000 888.888 99.000 92.000	***	*******	******	冰冰水	
0.000 1049.141 30.000 8.000 890570. ***********************************	351,000	3.618	ଜୁଜୁଜୁଜୁ	u)	Ø
361.000 3.346 0.000 51.735 0.000 371.000 3.0346 0.000 47.845 0.000 371.000 3.088 0.000 47.845 0.000 371.000 895.445 30.000 43.272 0.000 8.000 825.370 30.000 43.272 0.000 8.000 825.370 30.000 43.272 0.000 8.000 825.370 30.000 43.272 0.000 8.000 825.370 30.000 9.000 9.000 9.000 7.626 0.000 0.000 9.000 9.000 7.626 0.000 0.000 9.000 8.000 7.650 0.000 24.221 0.000 8.888 8.888 9.000 0.000 9.000 8.800 6.000 0.000 9.000 9.000 8.880 8.000 0.000 9.000 9.000 8.880 9.000 0.000 9.000 9.000 8.880 9.000 0.000 9.000 9.000 <td< th=""><th></th><th>1049,141</th><th>ଓଡ଼ି ଓଡ଼ିଆ</th><th><u>د</u></th><th>57. 80.</th></td<>		1049,141	ଓଡ଼ି ଓଡ଼ିଆ	<u>د</u>	57. 80.
######################################	* '\ * '\ *	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	**********	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	ß
**************************************	000.0 0.000	0000 0000 0000 0000	30°00'00'	0 0 0 0 0 0 0 0	200
371.000 3.088 0.000 47.845 0.000 ************************************	***	*	*****	**********	• •
0.000 895.445 30.000 905710. ************************************		9. 60 88	ଉ. ଉଉନ	47.845	Ġ
**************************************	ଜିନ୍ତି ନ	895,445	30.009	ଜିନ୍ତି ଓଡ଼ି	710.
9.000 73.676 9.000 825.370 9.000 37.891 9.000 37.891 9.000 2.433 8.000 2.433 9.000 921064 8.888 8.800 9.000 921064 8.888 8.800 9.000 924221 8.888 8.800 8.888 924221 9.000 924221 8.880 924221 8.888 8.880 8.800 924221 9.000 92433 8.800 924221 9.800 924221 8.800 926397 8.800 926397 8.800 926397 9.800 926397 9.800 926397 9.800 926397	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	*************************************	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	* ()	G
0.000 825.370 30.000 9.1000 911809.0 14.***********************************	100 100	0:10:11:11:11:11:11:11:11:11:11:11:11:11	200 · 0 ·	9	•
391.000 2.626 0.000 37.891 0.000 37.891 0.000 2.433 0.000 31.593 0.000 31.593 0.000 31.593 0.000 31.593 0.000 31.593 0.000 31.593 0.000 31.593 0.000 32.274 0.000 0.000 32.43164.		822°378	38	© 4	1889. *
6.000 761.503 30.000 916927. 401.000 2.433 6.000 31.593 6.2044. ************************************	391.666	**************************************	**************************************	κ Γ~-	ලේ *
######################################	ର. ଚତ୍ତ	761.503	30.000	9. ଉପର	16927.
#*************************************	., .	። ። ። ። ። ።		ં 😙	ح :
**************************************	:	705.530	39,866	୍ତି	964
**************************************	* *	* 0	水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水水	********	(
**************************************	20.00 Z	. (<u>(</u>) ()	2 G 2 G 3 G 7 G	⊅ 0 7 0 1 0 1 0	0 0 •
421.000 2.157 0.000 16.101 0.00 0.000	***) **	************	***********	N M
625.588 38.886 8.897. ************************************	421.888	2.157	ପ୍ରପ୍ର ପ	16.101	وي
**************************************	3 3 3	درا	36.666	ପ୍ରତ୍ର ପ୍ରତ୍ର	6397.
20 20 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	たい) 作 寸 作 作	* (\ *	米米米米米米米米米米米米米米米米	********	*
	9	100 NOV) () ()	VI (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0	֓֞֞֜֞֜֓֓֓֓֓֓֓֓֓֓֓֓֓֓֓֓֟֜֓֓֓֓֓֓֓֟֝

LIST OF REFERENCES

- 1. Valenti, A. M., Molder, S. and Salter, G. R., "Gun-Launching Supersonic-combustion Ramjets", Aeronautics and Aerospace Engineering, pp. 24-29, December 1963.
- Murphy, C. H., Bull, G. V. and Boyer, E. D., "Gun Launched Sounding Rockets and Projectiles", Annals of the New York Academy of Sciences, Vol 187, pp. 304-323, 25 January 1972.
- 3. Covault, C., "Antisatellite Weapon Design Advances", Aviation Week & Space Technology, pp. 243-247, 18 June 1980.
- 4. Johnson, N. L., "Orbital Phasing of Soviet Ocean Surveillance Satellites", Journal of Spacecraft and Rockets, Vol. 19, No. 2, p. 113, March-April 1982.
- 5. Archer, D. H. R. and Pretty, R. T., <u>Janes's Weapon</u>
 Systems, 1973-1974, p. 746, Sampson Low, Marston & Co.,
 1973.
- 6. Naval Ordnance Station Indian Head, Maryland Report 289, 16-inch, 280-MM Spin-stabilized Subcaliber Round Feasibility Program: Final Report, by Monetta, D. J., p. 9, 30 April 1969.
- 7. Ballistic Research Laboratories (BRL), Report No. 209, Supersonic Combustion Ramjet Flight Testing (Scram-jet), by Space Research Corp., February 1975.
- 8. Advisory Group for Aeronautical Research and Development, Combustion and Propulsion Fourth AGARD Colloquium, p. 84-155, Pergamon Press, 1961.
- 9. U. S. Department of Commerce Weather Bureau, U. S. Extension to the ICAO Standard Atmosphere Tables and Data to 300 Standard Geopotential Kilometers, by Minzer, R. A., Ripley, W. S. and Condron, T. P., 1958.
- 10. Wallace, F. B., "Air-Breathing Propulsion", Astronautics & Aeronautics, Vol. 18, No. 12, pp. 28-29, December 1980.
- 11. Truitt, R. W., Hypersonic Aerodynamics, pp. 64-104, Ronald Press, 1959.

- 12. Bertin, J. J. and Smith, M. L., <u>Aerodynamics for Engineers</u>, pp. 142-151, Prentice-Hall, 1979.
- 13. Morrison, P. H. and Amberntson, D. S., "Guidance and Control of a Cannon-Launched Guided Projectile", Journal of Spacecraft and Rockets, Vol. 14, No. 6, pp. 328-334, June 1977.

BIBLIOGRAPHY

Ballistic Research Laboratories (BRL), <u>Harp-Influence on</u> R & D Testing and Weapons Technology, by Murphy, C. H., 5 January 1969.

"Bremerton's Mothball Fleet", All Hands, No. 77, pp. 34-40, October 1981.

Bull, G. V. and Murphy, C. H., "Gun-Boosted Rockets for High Performance Sounding Missions", Proceedings of AIAA Sounding Rocket Vehicle Technology Conference, pp. 581-593, February, 1967.

Collar, A. R. and Tinker, J., Hypersonic Flow, Eleventh Symposium of the Colston Research Society, Briston 1959, Academic Press, 1960.

Cox, R. N. and Crabtree, L. F., Elements of Hypersonic Aerodynamics, Academic Press, 1965.

Directorate of Integration, Test and Operations U.S. Air Force, White Paper, Prototype Miniature Air-Launched Segment, 1 October 1979.

Fourth International Symposium on Air Breathing Engines, 4th, Orlando, Fl, 1979, American Institute of Aeronautics and Astronautics.

Hayes, W. D. and Probstein, R. F., Hypersonic Flow Theory, Inviscid Flow, 2nd Edition, Academic Press, 1965.

National Aero-Space Administration (NASA) SP-381, Aeronautical Propulsion, Lewis Research Center, 1975.

Shapiro, A. H., The Dynamics and Thermodynamics of Compressible Fluid Flow, Vol. 1, Ronald Press, 1953.

Tennent, J. H., "Bigger Punch for BB's - New Jersey Gets Tomahawk and Harpoon", Surface Warfare, Vol. 6, No. 10, pp. 2-11, October 1981.

Third International Symposium on Air Breathing Engines, Munich, Germany, 1976, Deutsche Gasellschaft Fur Luft-und Raumfahrt e. V. (DGLR).

INITIAL DISTRIBUTION LIST

		No.	Copies
1.	Def .se Technical Information Center Cameron Station Alexandria, Virginia 22314		2
2.	Library, Code 0142 Naval Postgraduate School Monterey, California 93940		2
3.	Department Chairman, Code 67 Department of Aeronautics Naval Postgraduate School Monterey, California 93940		1
4.	Distinguished Professor A. E. Fuhs Code 67Fu Department of Aeronautics Naval Postgraduate School Monterey, California 93940		2
5.	Dr. L. V. Schmidt Assistant Secretary of the Navy Assistant for Engineering Technology (R. E. and S) Pentagon 5E731 Washington, D.C. 20350		1
6.	Commanding Officer Naval Surface Weapons Center Dahlgren, Virginia 22448		1
7.	Commander, Naval Sea Systems Command Naval Sea Systems Command Headquarters Attn: Code 62Y Washington, D.C. 20362		1
8.	Colonel J. Randell, USAF Los Angeles Air Force Station Space Division P.O. Box 92960 World Wide Postal Center Los Angeles, California 90009		1

9.	Commanding Officer Navy Space Systems Command Bldg. 130 Los Angeles Air Force Station Los Angeles, California 90009	1
10.	LTC Rene Larriva, USMC Defense Advanced Research Project Agency 1400 Wilson Boulevard Arlington, Virginia 22209	1
11.	Commander Artillery Development Command Fort Sill, Oklahoma 73503	1
12.	Lieutenant Joseph J. Natale 2111 San Vito Circle Monterey, California 93940	4
13.	Dr. R. Kenneth Lobb, Director Naval Applications of Advanced Technology Center for Naval Analyses P. O. Box 11280 Alexandria, Virginia 22311	1
14.	Captain Roy Patterson, USN PME-106 Naval Electronic Systems Command Naval Electronic Systems Command Headquarters Washington, D.C. 20360	1
15.	RADM William E. Ramsey, USN OP-943 Navy Department Washington, D.C. 20350	1
16.	Dr. Fred Billig Applied Physics Lab The Johns Hopkins University APL/JHU John Hop Rd Laurel, Maryland 20810	1